

Amplitudes in $D=6$ $N=(1,1)$ SYM Theory

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JHEP 1404 (2014) 121, arXiv:1402.1024 [hep-th]
Phys.Lett. B 734 (2014) 111, arXiv:1404.6998 [hep-th]

Motivation

Maximal SYM

D=4 N=4

D=6 N=2

D=10 N=1

- **Partial or total cancellation of UV divergences (all bubble and triangle diagrams cancel)**
- **First UV divergent diagrams at $D=4+6/L$**
- **Conformal or dual conformal symmetry**
- **Common structure of the integrands**

Bern, Dixon & Co 10
Drummond, Henn, Korchemsky, Sokatchev
Arkani-Hamed 12

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BDS conjecture

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D=6 $[g^2] \sim \frac{1}{M^2}$

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Toy model for gravity

Color decomposition & Spinor helicity formalism

Color ordered amplitude

$$\mathcal{A}_n^{a_1 \dots a_n}(p_1^{\lambda_1} \dots p_n^{\lambda_n}) = \sum_{\sigma \in S_n/Z_n} \text{Tr}[\sigma(T^{a_1} \dots T^{a_n})] A_n(\sigma(p_1^{\lambda_1} \dots p_n^{\lambda_n})) + \mathcal{O}(1/N_c)$$

Planar Limit $N_c \rightarrow \infty$, $g_{YM}^2 \rightarrow 0$ and $g_{YM}^2 N_c$ - fixed

*Cheung, O'Connell 09,
Bern&Co 10*

Spinor helicity formalism

Momentum p^μ , $p^2 = 0$, $\mu = 0, \dots, 5$

$SO(5, 1)$

$$p_{AB} = p_\mu (\sigma^\mu)_{AB}, \quad p^{AB} = p^\mu (\bar{\sigma}_\mu)^{AB}$$

$$p^{AB} = \lambda^{Aa} \lambda_a^B, \quad p_{AB} = \tilde{\lambda}_{A\dot{a}} \tilde{\lambda}_{B\dot{a}}$$

$$SU(4)^* \xrightarrow{\lambda^{Aa}}$$

Little group in D=6:

$$SO(4) \simeq SU(2) \times SU(2)$$

Lorentz invariant structures:

$$\lambda(i)^{Aa} \tilde{\lambda}(j)_{A\dot{a}} \doteq \langle i_a | j_{\dot{a}} \rangle = [j_{\dot{a}} | i_a \rangle$$

$$\langle 1_a 2_b 3_c 4_d \rangle \doteq \epsilon_{ABCD} \lambda_1^{Aa} \lambda_2^{Bb} \lambda_3^{Cc} \lambda_4^{Dd}$$

$$[1_{\dot{a}} 2_{\dot{b}} 3_{\dot{c}} 4_{\dot{d}}] \doteq \epsilon^{ABCD} \tilde{\lambda}_{A,1}^{\dot{a}} \tilde{\lambda}_{B,2}^{\dot{b}} \tilde{\lambda}_{C,3}^{\dot{c}} \tilde{\lambda}_{D,4}^{\dot{d}}$$

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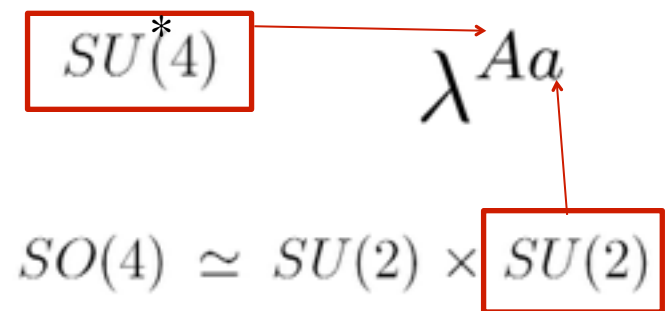
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Helicity is no longer conserved in D=6!



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Superfield formalism in D=6

$$\mathcal{N} = (1, 1) \text{ D=6 on-shell superspace} = \{\lambda_a^A, \tilde{\lambda}_{\dot{A}}, \eta_a^I, \bar{\eta}_{I'\dot{a}}\}$$

N=(1,1) on-shell states

Harmonic superspace
(*Dennen, Huang, Siegel 10*)

$$\frac{SU(2)_R}{U(1)} \times \frac{SU(2)_R}{U(1)}$$

$u_I^\mp$ and $\bar{u}^{\pm I'}$

$$q^{\mp A} = u_I^\mp q^{AI}, \quad \bar{q}_A^\pm = u^{\pm I'} \bar{q}_{AI'},$$

$$\eta_a^\mp = u_I^\mp \eta_a^I, \quad \bar{\eta}_{\dot{a}}^\pm = u^{\pm I'} \bar{\eta}_{I'\dot{a}},$$

$$\{q^{AI}, q^{BJ}\} = p^{AB} \epsilon^{IJ}$$

$$\{\bar{q}_{AI'}, \bar{q}_{BJ'}\} = p_{AB} \epsilon_{I'J'}$$

$$p^{AB} = \sum_i^n \lambda_i^{Aa} \lambda_{a,i}^B, \quad q^A = \sum_i^n \lambda_a^{A,i} \eta_i^a, \quad \bar{q}_A = \sum_i^n \tilde{\lambda}_{A,i}^{\dot{a}} \bar{\eta}_{\dot{a},i}$$

$$\Phi^{--}, \Phi^{-+}, \Phi^{+-}, \Phi^{++},$$

$$\Psi^{-a}, \Psi^{+a}, \bar{\Psi}^{-\dot{a}}, \bar{\Psi}^{+\dot{a}},$$

$$A^{a\dot{a}}$$

$$\{\lambda_a^A, \tilde{\lambda}_{\dot{A}}, \eta_a^-, \bar{\eta}_{\dot{a}}^+\}$$

The full amplitude

$$A_n(\{\lambda_a^A, \tilde{\lambda}_{\dot{A}}, \eta_a, \bar{\eta}_{\dot{a}}\}) = \delta^6(p^{AB}) \delta^4(q^A) \delta^4(\bar{q}_A) \mathcal{P}_n(\{\lambda_a^A, \tilde{\lambda}_{\dot{A}}, \eta_a, \bar{\eta}_{\dot{a}}\})$$

Grassmannian delta function is defined as:

$$\delta^4(q^A) = \frac{1}{4!} \epsilon_{ABCD} \delta\left(\sum_i^n q_i^A\right) \delta\left(\sum_k^n q_k^A\right) \delta\left(\sum_l^n q_l^A\right) \delta\left(\sum_p^n q_p^A\right)$$

The delta function always factorizes!

Polynomial of degree
2n-8 in Grassmannian variables

Tree level amplitude:

n=4

$$A_4^{(0)} = -ig_{YM}^2 \delta^6(p^{AB}) \frac{\delta^4(q^A) \delta^4(\bar{q}_A)}{st}$$

$$\mathcal{P}_4 = -i/st$$

In components

$$\mathcal{A}_4^{(0)}(1_{a\dot{a}} 2_{b\dot{b}} 3_{c\dot{c}} 4_{d\dot{d}}) = -ig_{YM}^2 \frac{\langle 1_a 2_b 3_c 4_d \rangle [1_{\dot{a}} 2_{\dot{b}} 3_{\dot{c}} 4_{\dot{d}}]}{st}$$

Perturbation Expansion for the Amplitudes

$$A_4/A_4^{tree}$$

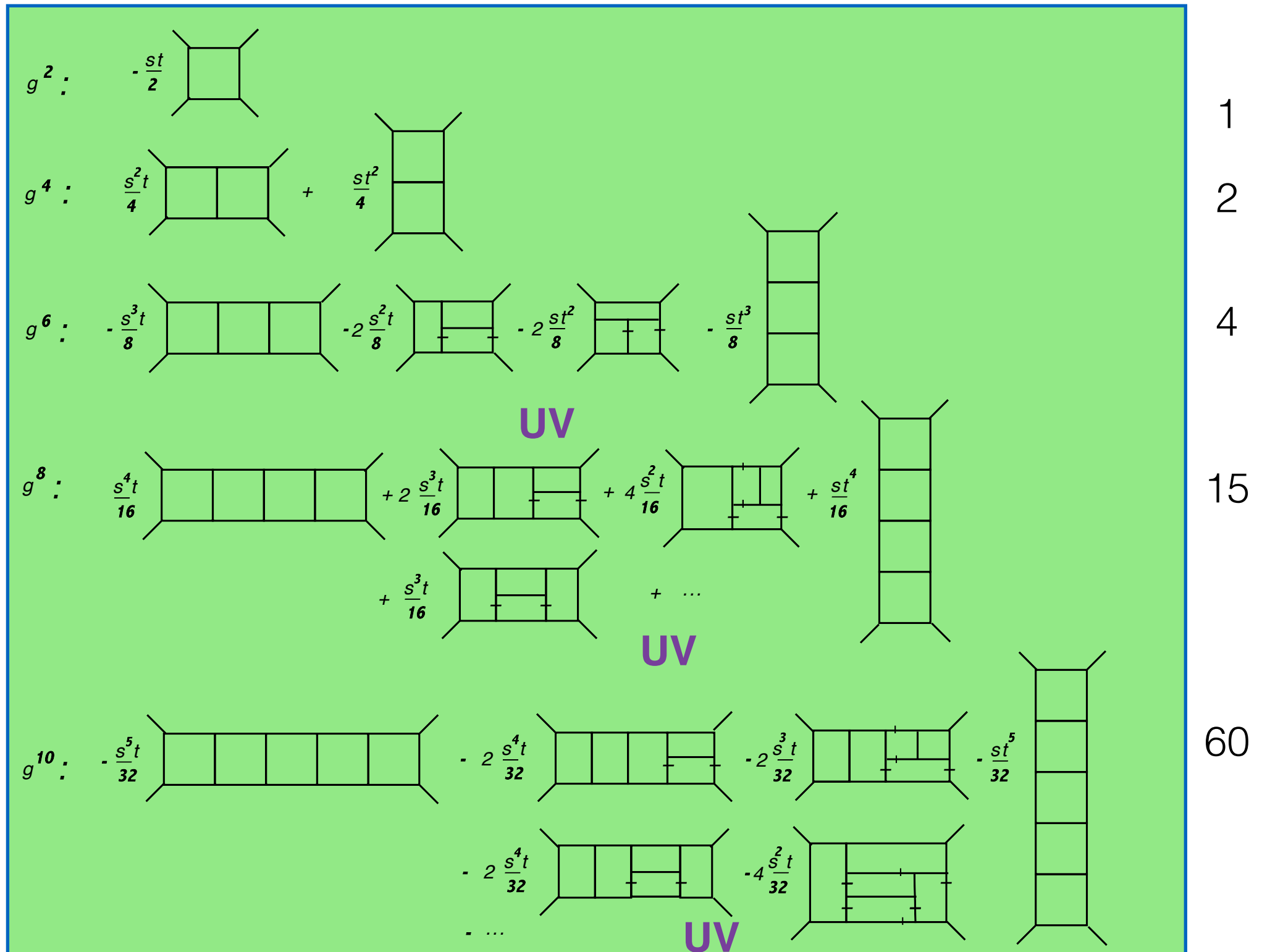
No bubbles
No Triangles

First UV div at
three loops

$$D=4+6/L$$

$$[g^2] \sim \frac{1}{M^2}$$

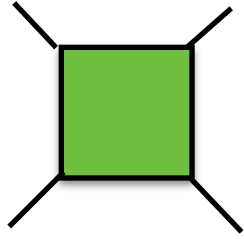
IR finite



Universal expansion for any D in maximal SYM

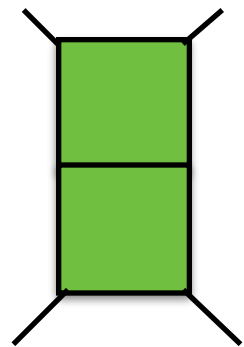
Perturbation Expansion for the Amplitudes

Exact calculation



$$p_i^2 = 0, \quad m = 0$$

$$B_1(s, t) = \frac{\pi^3}{(2\pi)^6} \frac{b_2(x)}{s+t}, \quad b_2(x) = \frac{L^2(x) + \pi^2}{2}, \quad L(x) \doteq \log(x), \quad x = \frac{t}{s}$$



$$B_2(s, t) = \left(\frac{\pi^3}{(2\pi)^6} \right)^2 \left(\frac{b_4(x)}{t} + \frac{b_3(x)}{s+t} \right)$$

Anastasiou, Tausk, Tejeda-Yeomans , 00
Bork, Kazakov, Vlasenko, 13

$$\begin{aligned} b_4(x) = & \left(2\zeta_3 - 2Li_3(-x) - \frac{\pi^2}{3}L(x) \right) L(1+x) + \left(\frac{1}{2}L(x) + \frac{\pi^2}{2} \right) L^2(1+x) \\ & + \left(2L(x)L(1+x) - \frac{\pi^2}{3} \right) Li_2(-x) + 2L(x)S_{1,2}(-x) - 2S_{2,2}(-x) \end{aligned}$$

$$b_3(x) = -2\zeta_3 + \frac{\pi^2}{3}L(x) - (L(x) + \pi^2) L(1+x) - 2L(x)Li_2(-x) + 2Li_3(-x)$$

Regge Limit $s \rightarrow \infty, \quad t < 0, \quad \text{fixed}$

$$B_1(s, t) \sim \frac{1}{2}L^2(x)$$

$$B_2(s, t) \sim \frac{1}{12}L^4(x)$$

Perturbation Expansion for the Amplitudes

Leading Logarithms

UV finite

Regge Limit $s \rightarrow \infty, \quad t < 0, \text{ fixed}$

$$B_n(t, s) \simeq \frac{1}{s} \frac{L^{2n}(x)}{n!(n+1)!}, \quad L \equiv \log(s/t)$$

Bork, Kazakov, Vlasenko, 13

$$\left. \frac{A_4}{A_4^{(0)}} \right|_{L.L.} = \sum_{n=0}^{\infty} \frac{(-g^2 t/2)^n L^{2n}(x)}{n!(n+1)!}, \quad \text{where } g^2 \equiv \frac{g_{YM}^2 N_c}{64\pi^3}.$$

$$\sum_{n=0}^{\infty} \frac{(-g^2 t/2)^n L^{2n}(x)}{n!(n+1)!} = \frac{I_1(2y)}{y}, \quad y \equiv \sqrt{g^2 |t|/2} L(x)$$

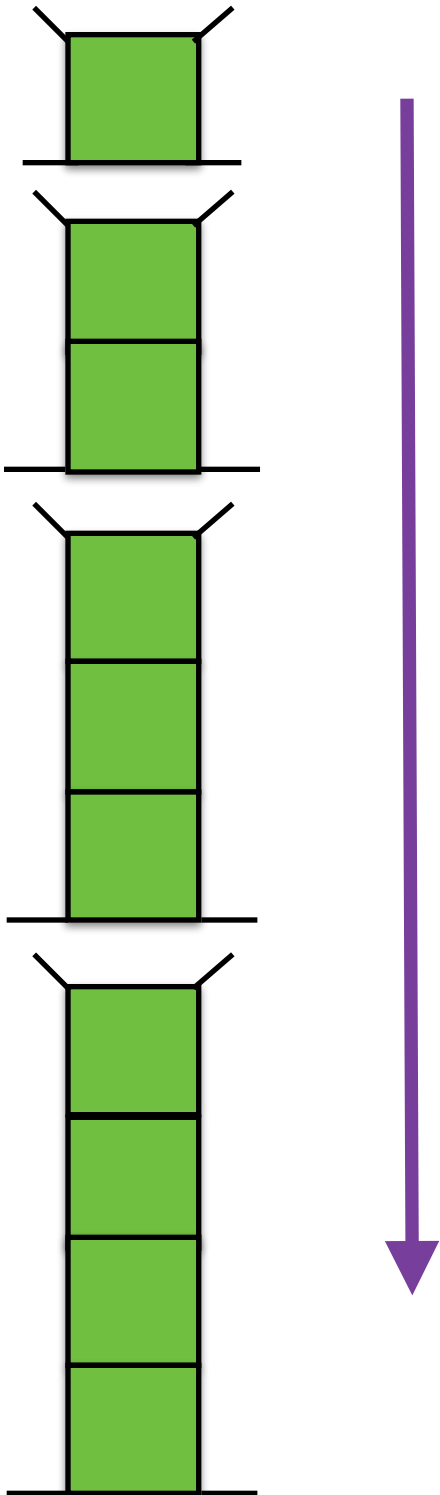
$$\left. \frac{A_4}{A_4^{(0)}} \right|_{L.L.} \sim \left(\frac{s}{t} \right)^{\alpha(t)-1}$$

!

Regge behaviour

Exact for $N_c \rightarrow \infty$

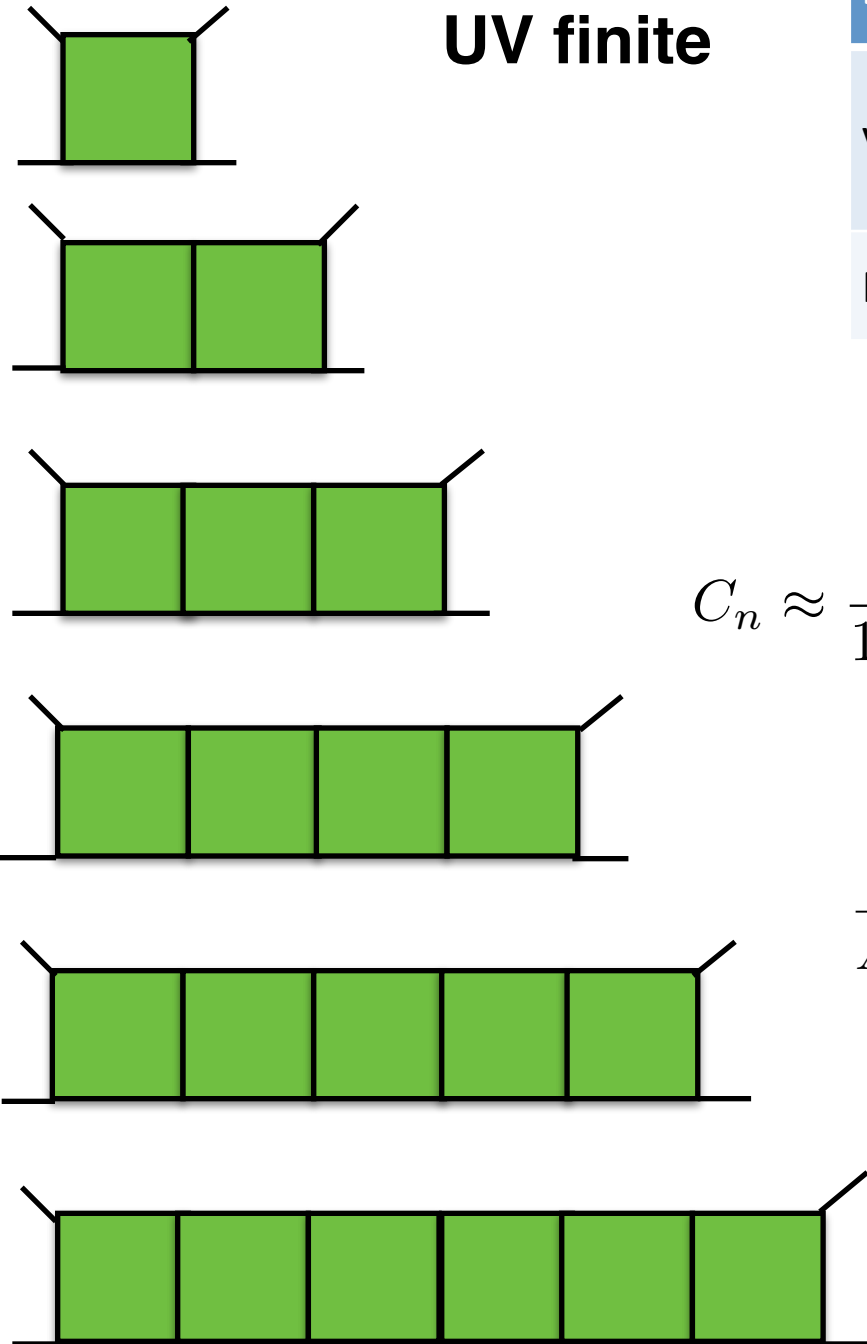
$$\alpha(t) = 1 + 2\sqrt{g^2 |t|/2} = 1 + \sqrt{\frac{g_{YM}^2 N_c |t|}{32\pi^3}}$$



Perturbation Expansion for the Amplitudes

Leading Powers

UV finite



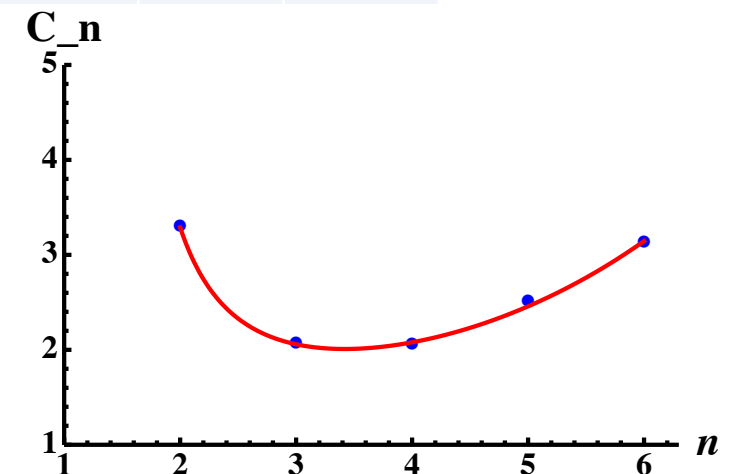
$$B_n(s, t) = \frac{1}{s} (C_n + O(t/s)), \quad n \geq 2$$

Kazakov, 14

Loops	1	2	3	4	5	6
Values						
Numerics						

Interpolation

$$C_n \approx \frac{1.63^n}{1.31n - 1.80} \approx 0.76 \frac{(\pi^2/6)^n}{n - 4/3}, \quad n \geq 2$$



$$\begin{aligned} \left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} &\approx -\frac{g^2 t}{2} \left[\frac{\pi^2}{2} - \sum_{n=2}^{\infty} 0.76 \frac{(-g^2 s/2)^{n-1} (\pi^2/6)^n}{n - 4/3} \right] \\ &= -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - 0.76 \frac{g^2 s \pi^2}{24} {}_2F_1\left(1, \frac{2}{3}, \frac{5}{3}, -\frac{g^2 s \pi^2}{12}\right) \right] \approx -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - \left(\frac{g^2 s}{2} \right)^{1/3} \right]. \end{aligned}$$

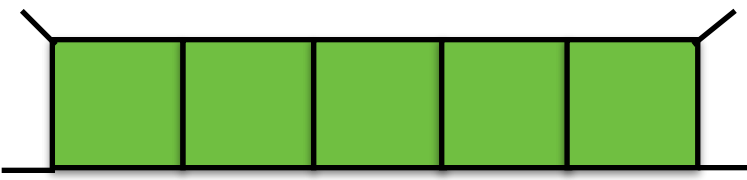
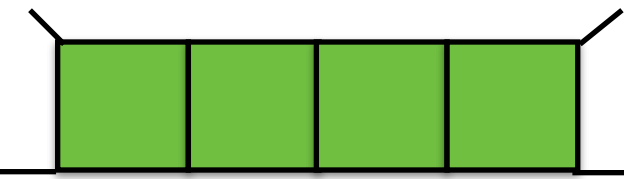
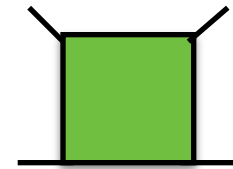
$$\left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} \approx g^2 t \frac{\pi^2}{4} \left(\frac{g^2 s}{2} \right)^{1/3}$$

!

Perturbation Expansion for the Amplitudes

Leading Powers

UV finite



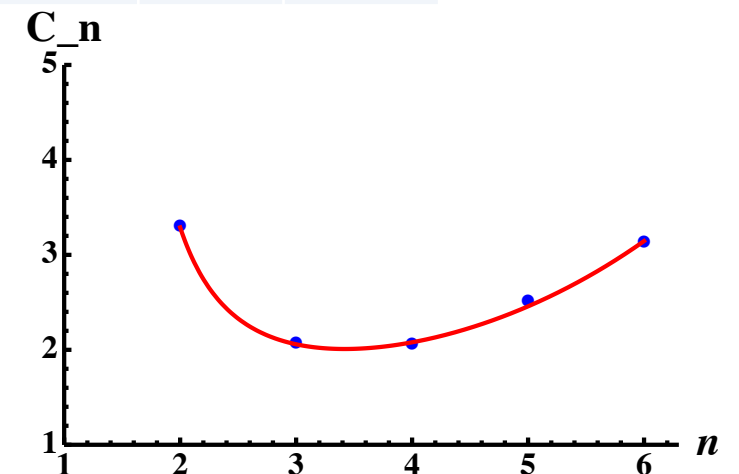
$$B_n(s, t) = \frac{1}{s} (C_n + O(t/s)), \quad n \geq 2$$

Kazakov, 14

Loops	1	2	3	4	5	6
Values	$\frac{\pi^2}{2}$					
Numerics						

Interpolation

$$C_n \approx \frac{1.63^n}{1.31n - 1.80} \approx 0.76 \frac{(\pi^2/6)^n}{n - 4/3}, \quad n \geq 2$$



$$\begin{aligned} \left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} &\approx -\frac{g^2 t}{2} \left[\frac{\pi^2}{2} - \sum_{n=2}^{\infty} 0.76 \frac{(-g^2 s/2)^{n-1} (\pi^2/6)^n}{n - 4/3} \right] \\ &= -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - 0.76 \frac{g^2 s \pi^2}{24} {}_2F_1\left(1, \frac{2}{3}, \frac{5}{3}, -\frac{g^2 s \pi^2}{12}\right) \right] \approx -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - \left(\frac{g^2 s}{2} \right)^{1/3} \right]. \end{aligned}$$

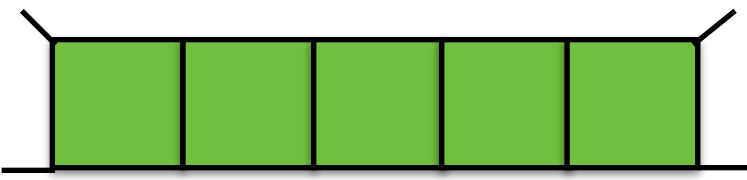
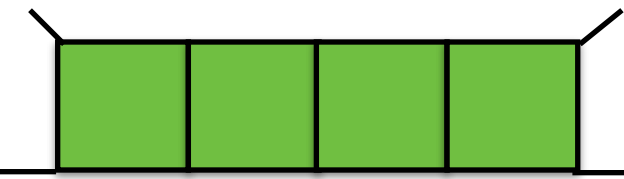
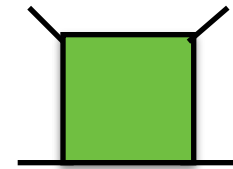
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Perturbation Expansion for the Amplitudes

Leading Powers

UV finite



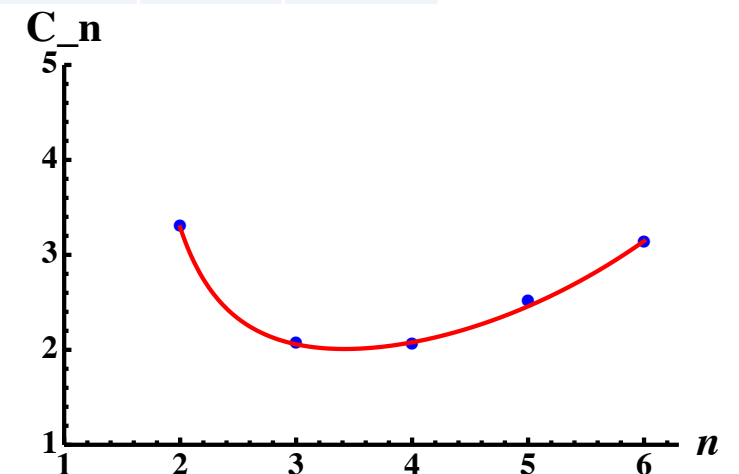
$$B_n(s, t) = \frac{1}{s} (C_n + O(t/s)), \quad n \geq 2$$

Kazakov, 14

Loops	1	2	3	4	5	6
Values	$\frac{\pi^2}{2}$	$\frac{\pi^2}{3}$				
Numerics						

Interpolation

$$C_n \approx \frac{1.63^n}{1.31n - 1.80} \approx 0.76 \frac{(\pi^2/6)^n}{n - 4/3}, \quad n \geq 2$$



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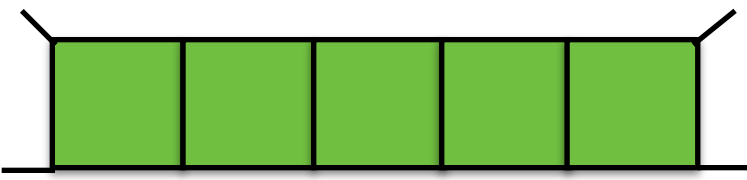
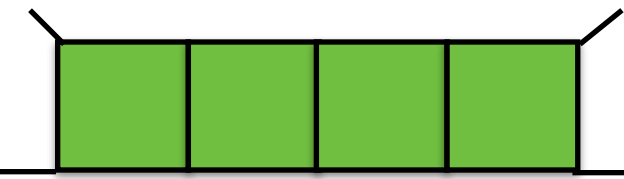
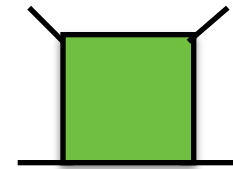
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Perturbation Expansion for the Amplitudes

Leading Powers

UV finite



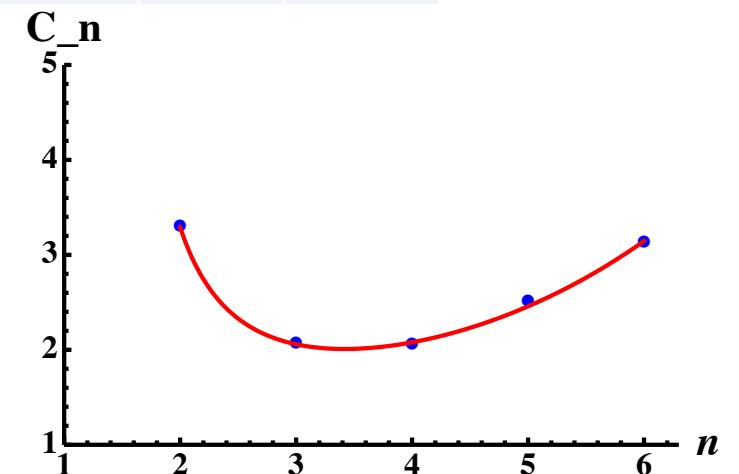
$$B_n(s, t) = \frac{1}{s} (C_n + O(t/s)), \quad n \geq 2$$

Kazakov, 14

Loops	1	2	3	4	5	6
Values	$\frac{\pi^2}{2}$	$\frac{\pi^2}{3}$	$-\pi^2 + \frac{31\pi^6}{1890}$ $-8\zeta_3 + 4\zeta_3^2$			
Numerics						

Interpolation

$$C_n \approx \frac{1.63^n}{1.31n - 1.80} \approx 0.76 \frac{(\pi^2/6)^n}{n - 4/3}, \quad n \geq 2$$



$$\begin{aligned} \left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} &\approx -\frac{g^2 t}{2} \left[\frac{\pi^2}{2} - \sum_{n=2}^{\infty} 0.76 \frac{(-g^2 s/2)^{n-1} (\pi^2/6)^n}{n - 4/3} \right] \\ &= -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - 0.76 \frac{g^2 s \pi^2}{24} {}_2F_1\left(1, \frac{2}{3}, \frac{5}{3}, -\frac{g^2 s \pi^2}{12}\right) \right] \approx -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - \left(\frac{g^2 s}{2} \right)^{1/3} \right]. \end{aligned}$$

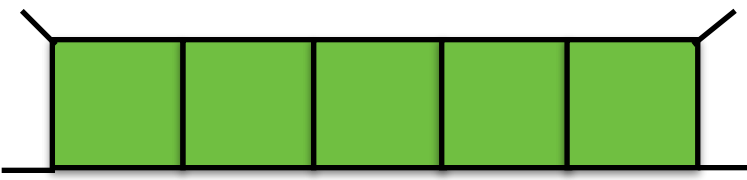
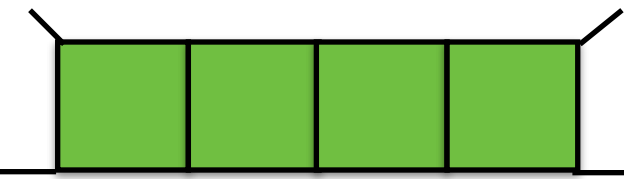
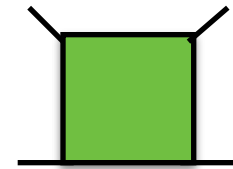
$$\left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} \approx g^2 t \frac{\pi^2}{4} \left(\frac{g^2 s}{2} \right)^{1/3}$$

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Perturbation Expansion for the Amplitudes

Leading Powers

UV finite



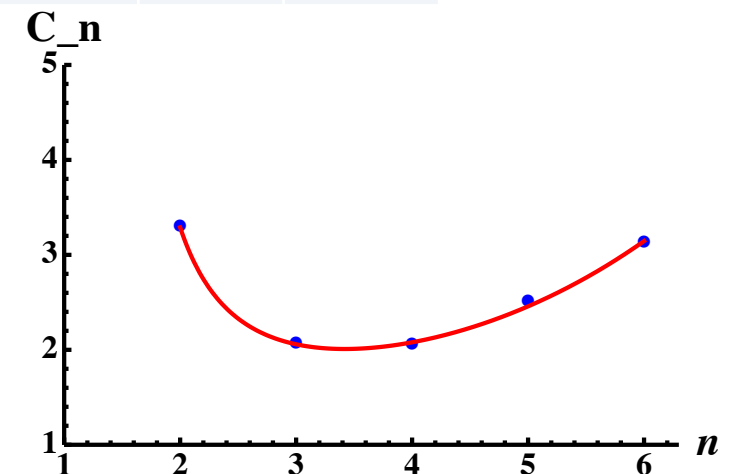
$$B_n(s, t) = \frac{1}{s} (C_n + O(t/s)), \quad n \geq 2$$

Kazakov, 14

Loops	1	2	3	4	5	6
Values	$\frac{\pi^2}{2}$	$\frac{\pi^2}{3}$	$-\pi^2 + \frac{31\pi^6}{1890} - 8\zeta_3 + 4\zeta_3^2$			
Numerics	4.93					

Interpolation

$$C_n \approx \frac{1.63^n}{1.31n - 1.80} \approx 0.76 \frac{(\pi^2/6)^n}{n - 4/3}, \quad n \geq 2$$



$$\begin{aligned} \left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} &\approx -\frac{g^2 t}{2} \left[\frac{\pi^2}{2} - \sum_{n=2}^{\infty} 0.76 \frac{(-g^2 s/2)^{n-1} (\pi^2/6)^n}{n - 4/3} \right] \\ &= -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - 0.76 \frac{g^2 s \pi^2}{24} {}_2F_1\left(1, \frac{2}{3}, \frac{5}{3}, -\frac{g^2 s \pi^2}{12}\right) \right] \approx -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - \left(\frac{g^2 s}{2} \right)^{1/3} \right]. \end{aligned}$$

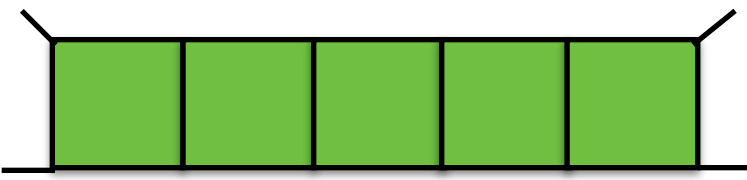
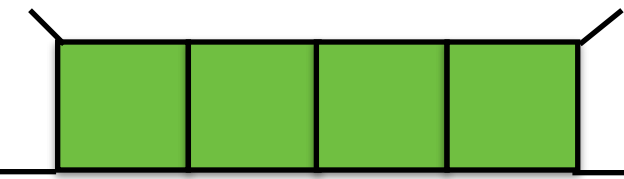
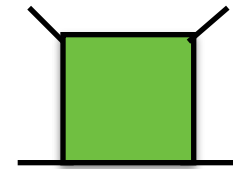
$$\left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} \approx g^2 t \frac{\pi^2}{4} \left(\frac{g^2 s}{2} \right)^{1/3}$$

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Perturbation Expansion for the Amplitudes

Leading Powers

UV finite



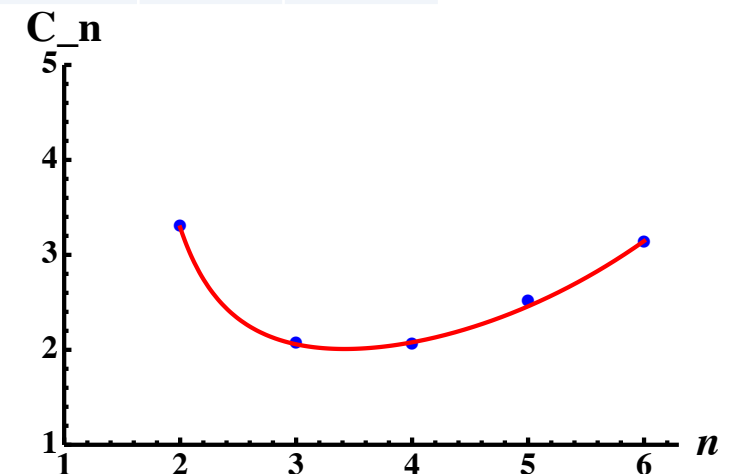
$$B_n(s, t) = \frac{1}{s} (C_n + O(t/s)), \quad n \geq 2$$

Kazakov, 14

Loops	1	2	3	4	5	6
Values	$\frac{\pi^2}{2}$	$\frac{\pi^2}{3}$	$-\pi^2 + \frac{31\pi^6}{1890}$ $-8\zeta_3 + 4\zeta_3^2$			
Numerics	4.93	3.29				

Interpolation

$$C_n \approx \frac{1.63^n}{1.31n - 1.80} \approx 0.76 \frac{(\pi^2/6)^n}{n - 4/3}, \quad n \geq 2$$



$$\begin{aligned} \left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} &\approx -\frac{g^2 t}{2} \left[\frac{\pi^2}{2} - \sum_{n=2}^{\infty} 0.76 \frac{(-g^2 s/2)^{n-1} (\pi^2/6)^n}{n - 4/3} \right] \\ &= -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - 0.76 \frac{g^2 s \pi^2}{24} {}_2F_1\left(1, \frac{2}{3}, \frac{5}{3}, -\frac{g^2 s \pi^2}{12}\right) \right] \approx -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - \left(\frac{g^2 s}{2} \right)^{1/3} \right]. \end{aligned}$$

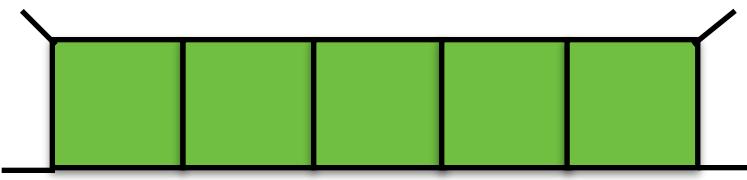
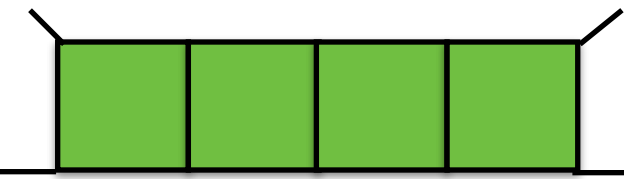
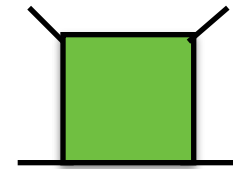
$$\left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} \approx g^2 t \frac{\pi^2}{4} \left(\frac{g^2 s}{2} \right)^{1/3}$$

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Perturbation Expansion for the Amplitudes

Leading Powers

UV finite



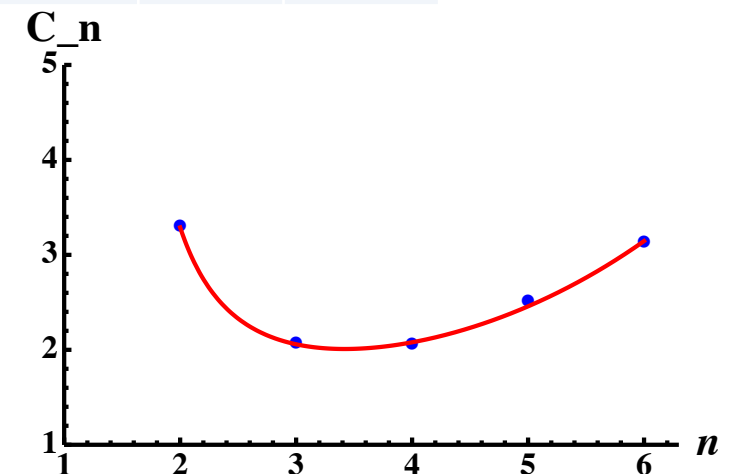
$$B_n(s, t) = \frac{1}{s} (C_n + O(t/s)), \quad n \geq 2$$

Kazakov, 14

Loops	1	2	3	4	5	6
Values	$\frac{\pi^2}{2}$	$\frac{\pi^2}{3}$	$-\pi^2 + \frac{31\pi^6}{1890}$ $-8\zeta_3 + 4\zeta_3^2$			
Numerics	4.93	3.29	2.06			

Interpolation

$$C_n \approx \frac{1.63^n}{1.31n - 1.80} \approx 0.76 \frac{(\pi^2/6)^n}{n - 4/3}, \quad n \geq 2$$



$$\begin{aligned} \left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} &\approx -\frac{g^2 t}{2} \left[\frac{\pi^2}{2} - \sum_{n=2}^{\infty} 0.76 \frac{(-g^2 s/2)^{n-1} (\pi^2/6)^n}{n - 4/3} \right] \\ &= -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - 0.76 \frac{g^2 s \pi^2}{24} {}_2F_1\left(1, \frac{2}{3}, \frac{5}{3}, -\frac{g^2 s \pi^2}{12}\right) \right] \approx -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - \left(\frac{g^2 s}{2} \right)^{1/3} \right]. \end{aligned}$$

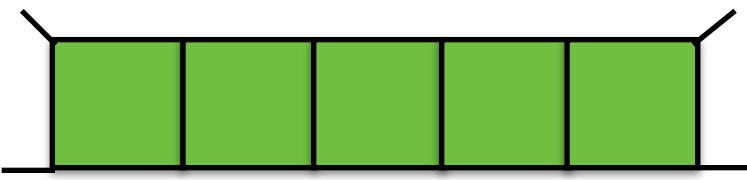
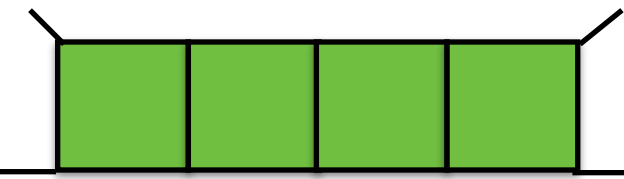
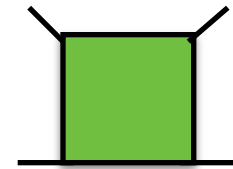
$$\left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} \approx g^2 t \frac{\pi^2}{4} \left(\frac{g^2 s}{2} \right)^{1/3}$$

!

Perturbation Expansion for the Amplitudes

Leading Powers

UV finite



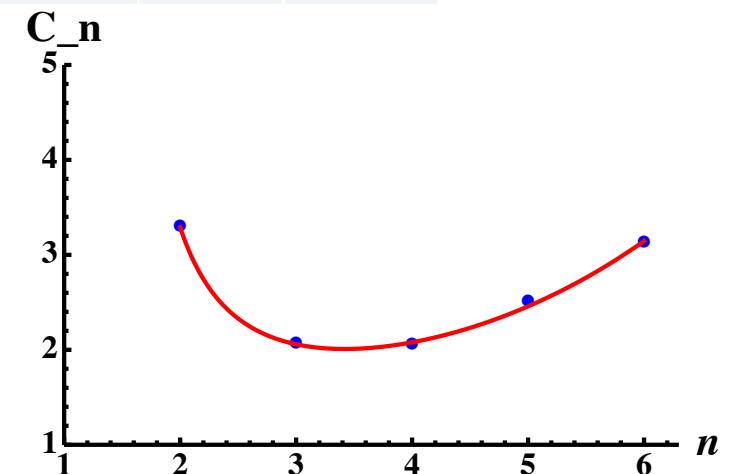
$$B_n(s, t) = \frac{1}{s} (C_n + O(t/s)), \quad n \geq 2$$

Kazakov, 14

Loops	1	2	3	4	5	6
Values	$\frac{\pi^2}{2}$	$\frac{\pi^2}{3}$	$-\pi^2 + \frac{31\pi^6}{1890}$ $-8\zeta_3 + 4\zeta_3^2$			
Numerics	4.93	3.29	2.06	2.05		

Interpolation

$$C_n \approx \frac{1.63^n}{1.31n - 1.80} \approx 0.76 \frac{(\pi^2/6)^n}{n - 4/3}, \quad n \geq 2$$



$$\begin{aligned} \left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} &\approx -\frac{g^2 t}{2} \left[\frac{\pi^2}{2} - \sum_{n=2}^{\infty} 0.76 \frac{(-g^2 s/2)^{n-1} (\pi^2/6)^n}{n - 4/3} \right] \\ &= -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - 0.76 \frac{g^2 s \pi^2}{24} {}_2F_1\left(1, \frac{2}{3}, \frac{5}{3}, -\frac{g^2 s \pi^2}{12}\right) \right] \approx -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - \left(\frac{g^2 s}{2} \right)^{1/3} \right]. \end{aligned}$$

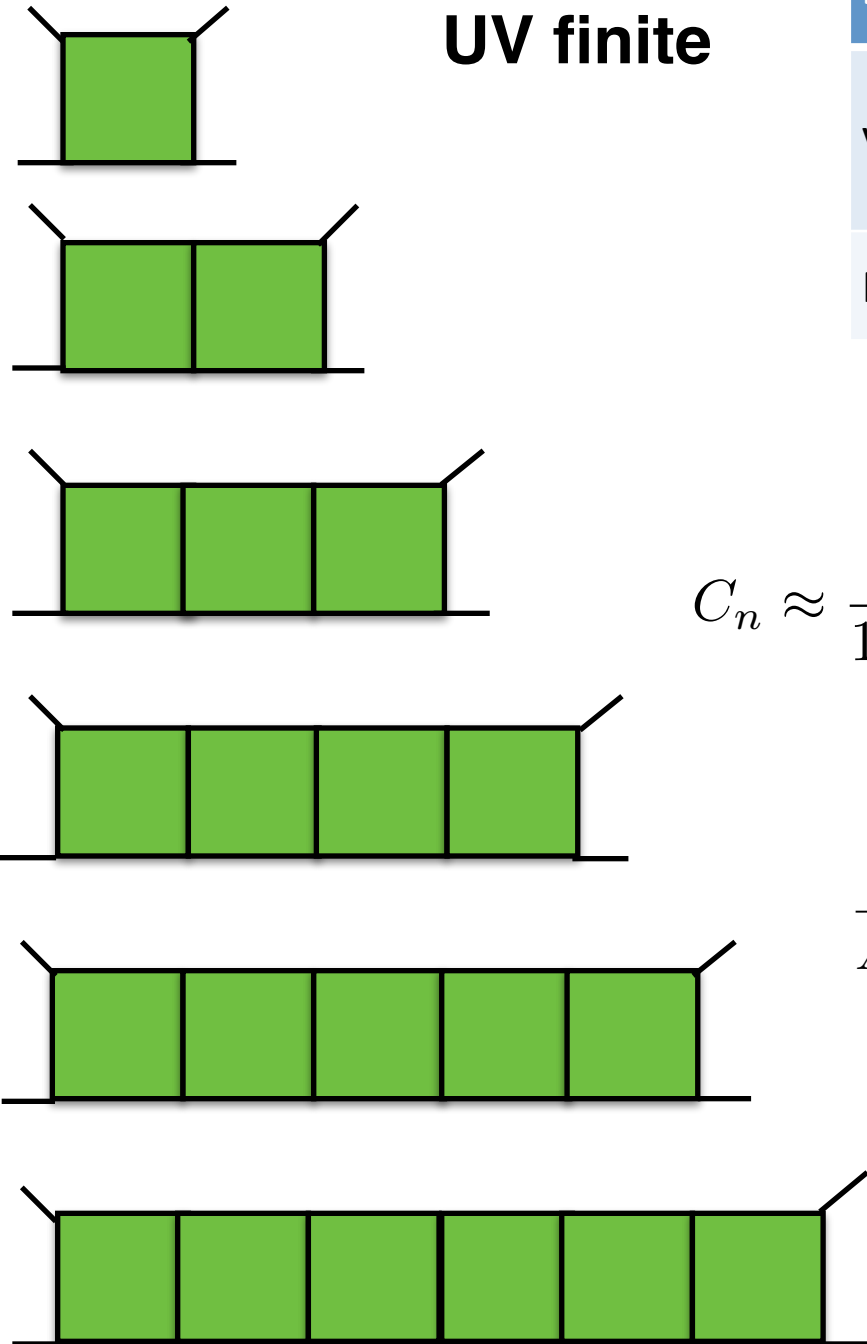
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Perturbation Expansion for the Amplitudes

Leading Powers

UV finite



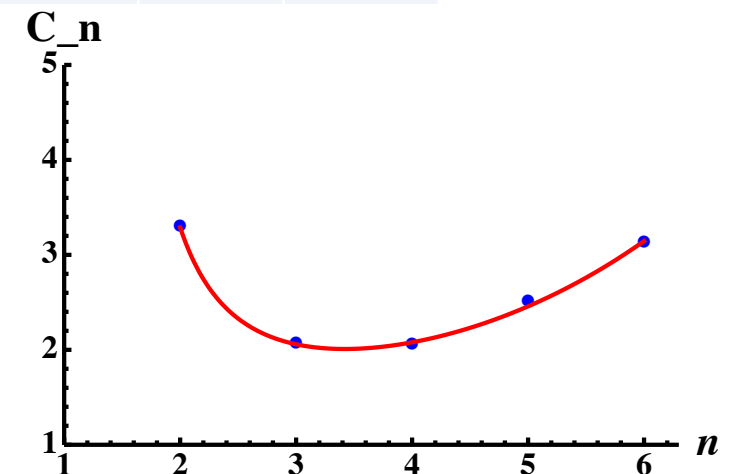
$$B_n(s, t) = \frac{1}{s} (C_n + O(t/s)), \quad n \geq 2$$

Kazakov, 14

Loops	1	2	3	4	5	6
Values	$\frac{\pi^2}{2}$	$\frac{\pi^2}{3}$	$-\pi^2 + \frac{31\pi^6}{1890}$ $-8\zeta_3 + 4\zeta_3^2$			
Numerics	4.93	3.29	2.06	2.05	2.42	

Interpolation

$$C_n \approx \frac{1.63^n}{1.31n - 1.80} \approx 0.76 \frac{(\pi^2/6)^n}{n - 4/3}, \quad n \geq 2$$



$$\begin{aligned} \left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} &\approx -\frac{g^2 t}{2} \left[\frac{\pi^2}{2} - \sum_{n=2}^{\infty} 0.76 \frac{(-g^2 s/2)^{n-1} (\pi^2/6)^n}{n - 4/3} \right] \\ &= -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - 0.76 \frac{g^2 s \pi^2}{24} {}_2F_1\left(1, \frac{2}{3}, \frac{5}{3}, -\frac{g^2 s \pi^2}{12}\right) \right] \approx -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - \left(\frac{g^2 s}{2} \right)^{1/3} \right]. \end{aligned}$$

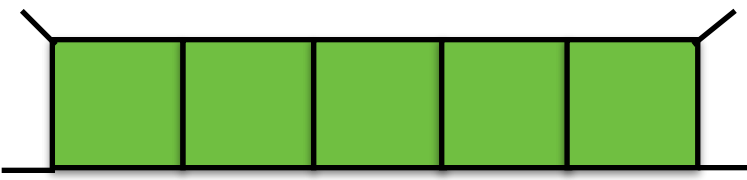
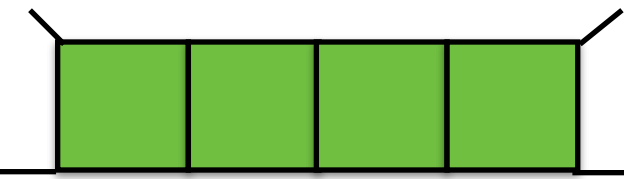
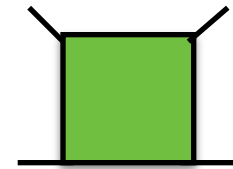
$$\left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} \approx g^2 t \frac{\pi^2}{4} \left(\frac{g^2 s}{2} \right)^{1/3}$$

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Perturbation Expansion for the Amplitudes

Leading Powers

UV finite



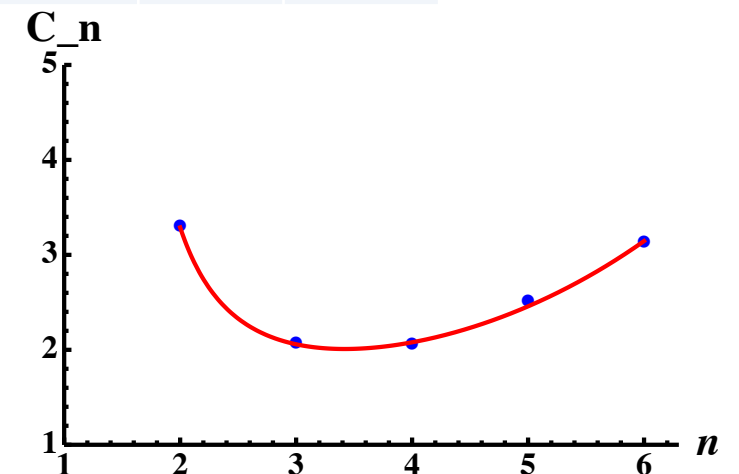
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Kazakov, 14

Loops	1	2	3	4	5	6
Values	$\frac{\pi^2}{2}$	$\frac{\pi^2}{3}$	$-\pi^2 + \frac{31\pi^6}{1890}$ $-8\zeta_3 + 4\zeta_3^2$			
Numerics	4.93	3.29	2.06	2.05	2.42	3.13

Interpolation

$$C_n \approx \frac{1.63^n}{1.31n - 1.80} \approx 0.76 \frac{(\pi^2/6)^n}{n - 4/3}, \quad n \geq 2$$



$$\begin{aligned} \left. \frac{A_4}{A_4^{(0)}} \right|_{L.P.} &\approx -\frac{g^2 t}{2} \left[\frac{\pi^2}{2} - \sum_{n=2}^{\infty} 0.76 \frac{(-g^2 s/2)^{n-1} (\pi^2/6)^n}{n - 4/3} \right] \\ &= -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - 0.76 \frac{g^2 s \pi^2}{24} {}_2F_1\left(1, \frac{2}{3}, \frac{5}{3}, -\frac{g^2 s \pi^2}{12}\right) \right] \approx -\frac{g^2 t}{2} \frac{\pi^2}{2} \left[1 - \left(\frac{g^2 s}{2} \right)^{1/3} \right]. \end{aligned}$$

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!

Perturbation Expansion for the Amplitudes

Leading Divergences

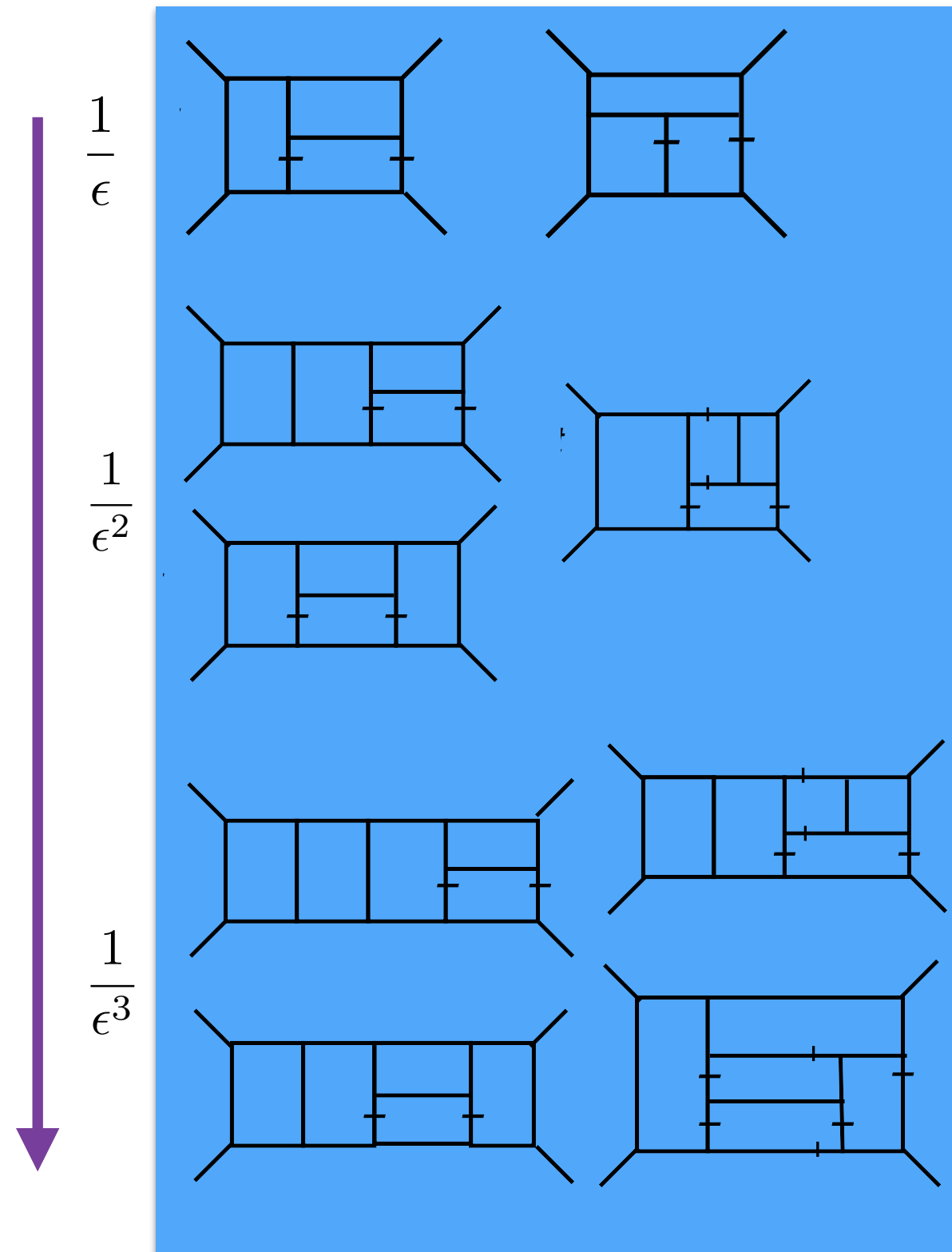
Loops	Combinatorics	Divergence
3	$(-g^2 s/2)^3 \quad 2t/s$	$1/6\epsilon$
4	$(-g^2 s/2)^4 \quad 2t/s$	$1/36\epsilon^2$
5	$(-g^2 s/2)^5 \quad 2t/s$	$1/216\epsilon^3$

Geom progression !?

$$\left. \frac{A_4}{A_4^{(0)}} \right|_{\text{Leading Div.}} = 2 \frac{t}{s} \sum_{n=1}^{\infty} \left(-\frac{g^2 s}{2} \right)^{n+2} \left(\frac{1}{6\epsilon} \right)^n = 2 \frac{t}{s} \left(-\frac{g^2 s}{2} \right)^2 \frac{\frac{-g^2 s}{12\epsilon}}{1 + \frac{g^2 s}{12\epsilon}}$$

$$\epsilon \rightarrow +0$$

$$\left. \frac{A_4}{A_4^{(0)}} \right|_{\text{Leading Div.}} \rightarrow -2 \frac{t}{s} \left(-\frac{g^2 s}{2} \right)^2 = -\frac{g^4 s t}{2}$$



Perturbation Expansion for the Amplitudes

Leading Divergences

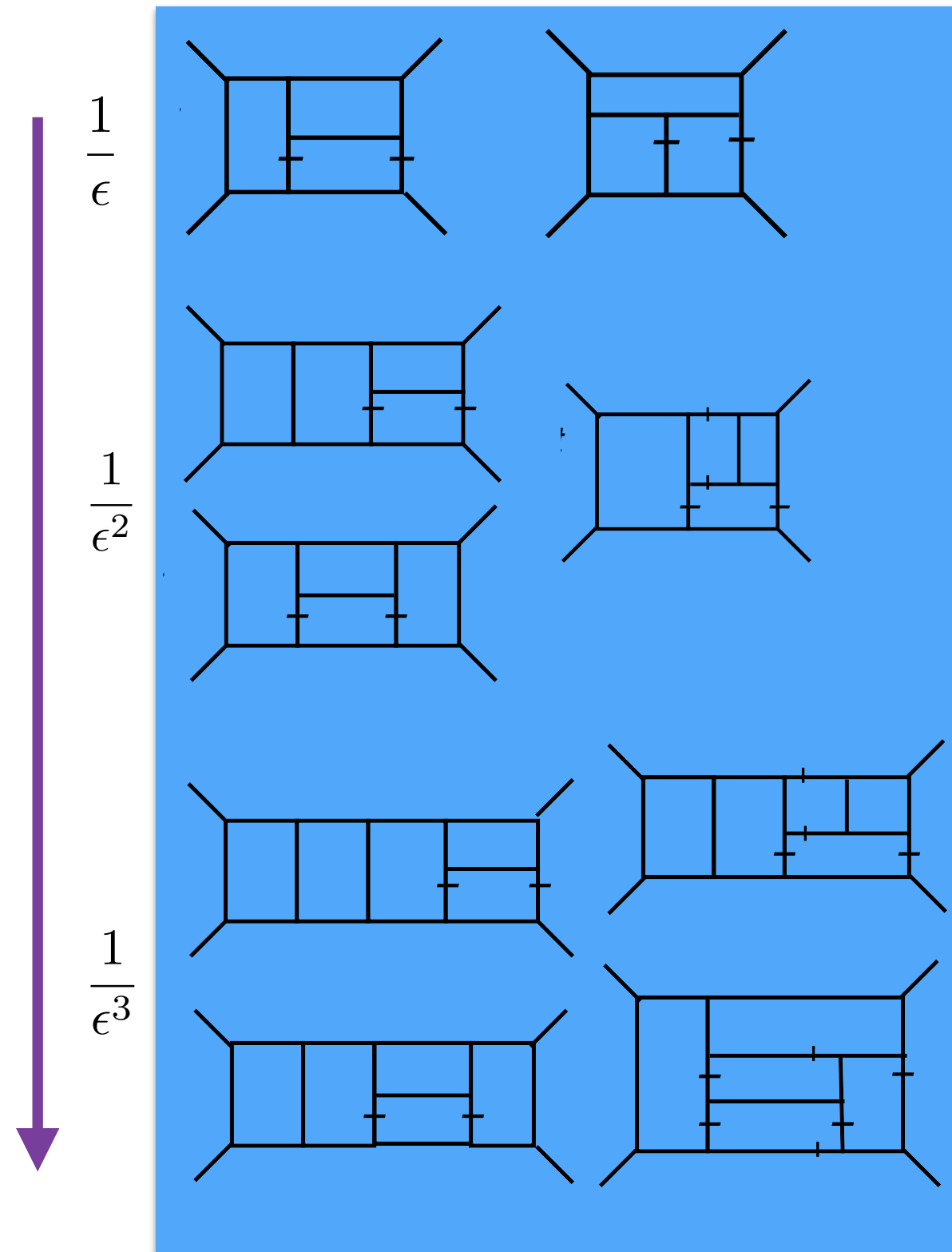
Loops	Combinatorics	Divergence
3	$(-g^2 s/2)^3 2t/s$	$1/6\epsilon$
4	$(-g^2 s/2)^4 2t/s$	$1/36\epsilon^2$
5	$(-g^2 s/2)^5 2t/s$	$1/216\epsilon^3$

Geom progression !?

$$\left. \frac{A_4}{A_4^{(0)}} \right|_{\text{Leading Div.}} = 2 \frac{t}{s} \sum_{n=1}^{\infty} \left(-\frac{g^2 s}{2} \right)^{n+2} \left(\frac{1}{6\epsilon} \right)^n = 2 \frac{t}{s} \left(-\frac{g^2 s}{2} \right)^2 \frac{\frac{-g^2 s}{12\epsilon}}{1 + \frac{g^2 s}{12\epsilon}}$$

$$\epsilon \rightarrow +0$$

$$\left. \frac{A_4}{A_4^{(0)}} \right|_{\text{Leading Div.}} \rightarrow -2 \frac{t}{s} \left(-\frac{g^2 s}{2} \right)^2 = -\frac{g^4 s t}{2}$$



In the limit $\epsilon \rightarrow 0$ the full expression is FINITE !

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- 🔗 In order to understand the nonrenormalizable theories one has to find an alternative description.
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