# Once again about the 4th generation of quarks and leptons

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# **Three generations conformism**

#### LEP – 3 neutrinos

- Tevatron no extra quarks
- LEP electroweak fits exclude extra generations (PDG08 J. Erler, P. Langacker "An extra generation of ordinary fermions is excluded at the 99.6% CL ...")
- Electroweak fits require light Higgs

# Leptop non-conformism

- LEPTOP approach to EWRC worked out by V.A.N., L.B. Okun, A.N. Rozanov and M.I. Vysotsky in the 90s.
- Phys. Lett. B 476 (2000) 107-115
- Phys. Lett. B 572 (2002) 111-116

Using LEPTOP it was found that the precision data do not exclude an existence of additional generation of quarks and leptons.

V.A.N., A.N. Rozanov, M.I. Vysotsky arXiv:0904.4570 (hep-ph)

Not excluded yet

. . . . . . .

Contradictions with New Bible – PDG booklet– claim (2008):

- There is no room for 4th generation of quark and leptons. It is excluded by precision data at the  $6\sigma$  level.
- Precision data prefer a light higgs

$$m_H = 84^{+32}_{-24} \text{ GeV}$$

Very soon LHC will fix  $N_g = 3$  or  $N_g = 4!$ 

#### Last chance to give this talk!!

## **General introduction**

Two strategies to look for a New Physics beyond the SM

#### Direct -LEP and Tevatron search for 4th generation– No trace of a New Physics L3 $m_E \gtrsim 100.8 \text{ GeV}$ decay to $\nu$ W; CDF, D0 $m_T \gtrsim 335 \text{ GeV}, m_B \gtrsim 338 \text{ Gev}$ (CC decay); $m_T \gtrsim 220 \text{ GeV}, m_B \gtrsim 190 \text{ Gev}$ (quasi-stable)

Indirect searches –

Precision experiment v.s. Precision calculations. Sometimes it works!

#### Neptune discovery (Le Verrier, Adams, Galle) (1846)

"Neptune was the first planet found by mathematical prediction rather than by empirical observation" (Wikipedia)

# Radiative corrections in the SM

- Interaction in the SM is mediated by gauge bosons exchange.
- Gauge bosons interact in a universal way with any particles, both the standard ones and the new ones.
- If the new particles do not mix with SM particles there are only "oblique" corrections to SM observables

 $\downarrow$ 

Corrections to the propagation of gauge fields only (to self-energy ):

$$\left\{ \begin{array}{l} \text{gauge field} \\ \text{propagator} \end{array} \right\} \equiv G(q^2) = \frac{g_0^2}{q^2 - m_0^2 - \Sigma(q^2)}$$

# **Decoupling of Heavy d.o.f.**

Decoupling of Heavy d.o.f. from Low-Energy Physics

- QED Berestetsky, Krokhin, Klebnikov (1956)
- Vector-like theories Appelquist–Carazzone Theorem (1975)

#### "Proof" in QED

Let renormalization procedure respects gauge-invariance:

• Photon is massless and propagator has a pole at  $q^2 = 0$ 

$$G(q^2) = \frac{e_0^2}{q^2(1 - \Pi(q^2))}$$

In equation  $G(q^2) = g_0^2/(q^2 - m_0^2 - \Sigma(q^2))$  we take  $m_0^2 = 0, \quad \Sigma(q^2) = q^2 \Pi(q^2)$ 

and assume that  $\Pi(q^2)$  is regular near  $q^2 = 0$ .

All particles have one and the same electric charge:

$$G(q^2) = \frac{e^2}{q^2}$$

for small  $q^2$  (large distance). It means that  $\Pi(0) \equiv 0$  for any particles! Thus

$$\Pi(q^2) \sim q^2$$

at  $q^2 \sim 0$ .

# Two step proof of decoupling

The contribution of heavy degrees of freedom into low-energy observables is suppressed by some power if these observables are expressed in terms of renormalized electric charge!

1) First step-dimension argument.

 $[\Pi(q^2)] = (m^2)^0$ 

2) Second step-universality of gauge couplings.

 $\Pi(q^2) \sim q^2$ 

Thus  $\delta \Pi(q^2) \sim q^2/m_{\text{heavy}}^2$  for small  $q^2$ . Heavy d.o.f. decouples from low-energy observables!

# g-2 in QED

New particles contribute into anomalous magnetic moment of leptons at the level of two loops :

$$a_{l} = \frac{1}{2}(g_{l} - 2) = \frac{\alpha}{2\pi} + O(\alpha^{2} \frac{m_{l}^{2}}{m_{heavy}^{2}})..$$

Though Berestetsky et al. (1956) argued

$$\delta a_e \sim \alpha^2 \left( \frac{m_e^2}{m_{heavy}^2} \right), \quad \delta a_\mu \sim \alpha^2 \left( \frac{m_\mu^2}{m_{heavy}^2} \right)$$

Enhancement factor  $(m_{\mu}^2/m_e^2) \sim 4 \cdot 10^4$ 

(g-2) of muon is more suitable for New Physics search.

# The electron g-2

What was correct on 60th is not absolutely correct now !! Theory

4-loop contribution into  $a_e$  including  $\mu, \tau$ , hadronic and weak loops

$$a_e^{th} = 1\ 159.652\ 172\ 99(930) \cdot 10^{-6}$$

#### Experiment

Harvard University experiment (2006) (2008)

$$a_e^{th} = 1\ 159.652\ 180\ 73(28)\cdot 10^{-6}$$

Accuracy 0.24 ppb!!

Need 5-loop calculation to be sensitive to 1TeV scale!

# The muon g-2

BNL precision experiment E821 on muon anomalous magnetic moment Theory *vs* Experiment Long history of mistakes:

1. CERN experiment (1975)

found missing light-by-light contribution into theoretical calculations of  $a_{\mu}$ .

2. BNL experiment (2004)

found wrong sign in classical Kinoshita calculation (1995) of hadronic contribution into light-by-light calculation

As a result  $7\sigma \rightarrow 3\sigma$  discrepancy.

# SM vs Exp.

Standard model theory and experiment comparison (in units  $10^{-11}$ )

QED 4-loops and some of 5-loops116 584 718.1 (Hadronic contribution to vacuum polarization6 903.0 (52.6)light-by-light116.0 (39.0)Weak 2-loops153.2 (1.8)Theory116 591 790.0 (Experiment116 592 080.0 (Exp.-Theory  $3.2\sigma$ 290.0 (90.3)

# **Current Status of muon (g-2)**

#### **Discrepancy with theory**

- 3.2 $\sigma$  if  $\alpha(m_{\mu})$  is calculated using low-energy  $e^+e^-$  data
- 1.4 $\sigma$  if  $\alpha(m_{\mu})$  is calculated using data on  $\tau$ -decay into hadrons

# No decoupling in the SM

An example – the third generation:

$$\left(\begin{array}{c} t\\b\end{array}\right)$$
 with  $m_t \gg m_b$ 

Thus for low-energy scattering ( $E \ll m_t$ ) we have direct violation of  $SU(2) \times U(1)$  symmetry

Effective nonrenormalizable theory  $\downarrow$ Power divergencies  $\sim \Lambda^2/m_W^2$  Natural cut-off  $\Lambda \sim m_t$ 

Thus EWRC depend on top quark mass as

$$\alpha \left( m_t^2/m_W^2 \right)$$
,  $\alpha^2 \left( m_t^2/m_W^2 \right)^2$  etc.  
 $\Downarrow$   
In this way top quark was found.

(Partly the same is true for c-quark.)

#### Degenerate case

$$\begin{pmatrix} U \\ D \end{pmatrix}$$
 with  $m_U \to \infty$ ;  $m_D \to \infty$ ;  $m_U - m_D = \text{finite}$ 

In this case we have finite non-zero contribution into observables.

# **General theory of a heavy d.o.f.**

Peskin and Takeuchi (1990, 1992) Contributions of New Physics can be hidden into universal three variables S, T and U.

$$S = 16\pi \left[ \Sigma'_A(0) - \Sigma'_V(0) \right]$$

$$T = \frac{4\pi}{s^2 m_W^2} \left[ \Sigma_{11}(0) - \Sigma_{33}(0) \right]$$

$$U = 16\pi \left[ \Sigma_{11}'(0) - \Sigma_{33}'(0) \right]$$

This approach equivalent to Effective Field Theory for low-energy d.o.f.

PDG claims that using S, T U analysis one can't find a room for the fourth generation.

# Main body of the talk

# LEPTOP 2009 fit

Observable	Exper. data	LEPTOP fit	Pull
$\Gamma_Z$ , GeV	2.4952(23)	2.4963(15)	-0.5
$\sigma_h$ , nb	41.540(37)	41.476(14)	1.8
$R_l$	20.771(25)	20.743(18)	1.1
$A^l_{ m FB}$	0.0171(10)	0.0164(2)	0.8
$A_{ au}$	0.1439(43)	0.1480(11)	-0.9
$R_b$	0.2163(7)	0.2158(1)	0.7
$R_c$	0.172(3)	0.1722(1)	-0.0
$A^b_{ m FB}$	0.0992(16)	0.1037(7)	-2.8
$A^c_{ m FB}$	0.0707(35)	0.0741(6)	-1.0
$s_l^2$ ( $Q_{ m FB}$ )	0.2324(12)	0.2314(1)	0.8

Observable	Exper. data	LEPTOP fit	Pull
$A_{\rm LR}$	0.1513(21)	0.1479(11)	1.6
$A_b$	0.923(20)	0.9349(1)	-0.6
$A_c$	0.670(27)	0.6682(5)	0.1
$m_W$ , GeV	80.398(25)	80.377(17)	0.9
$m_t$ , GeV	172.6(1.4)	172.7(1.4)	-0.1
$M_{ m H}$ , GeV		$84^{+32}_{-24}$	
$\hat{lpha}_s$		0.1184(27)	
$1/\bar{lpha}$	128.954(48)	128.940(46)	0.3
$\chi^2/n_{\rm d.o.f.}$		18.1/12	

# Fits with the fourth generation

- Suppose that mixing is small.
- Separate steep and flat directions in the dependence of  $\chi^2$  over new particle masses (V.A. Novikov et al. (2002))
- Fix  $m_U + m_D = 600$  GeV to avoid Tevatron direct search bounds; fix  $m_E = 200$  GeV; vary the difference of neutral lepton mass and the difference of Up- and Down-quark masses.

The results of the fit are presented in Fig. 1 for  $m_H = 120$  GeV, in Fig. 2 for  $m_H = 600$  GeV, and in Fig. 3 for  $m_H = 1000$  GeV.







- Quality of the fit with extra generation is good and is not worse than the Standard Model fit without additional generation.
- New generation removes upper bound on heavy Higgs

# How many extra generations?

• To simplify analysis we assume degeneracy of new particles with identical quantum numbers:  $m_{E_1} = m_{E_2} = ..., m_{N_1} = m_{N_2} = ..., m_{U_1} = m_{U_2} = ...,$ 

 $m_{D_1} = m_{D_2} = \dots$ 

- To study this problem we fix  $m_E = 200$  GeV,  $m_U = m_D = 300$  GeV.
- **•** Take  $m_H > 114$  GeV.

The levels of  $\chi^2$  are shown in Fig. 4.



The value of  $\chi^2$  for Standard Model and for  $N_g = 1$  are almost the same, while three and more additional generations are strongly excluded.

# $\mathbf{S}, \mathbf{T}, \mathbf{U} \text{ versus } \mathbf{V}_m, \mathbf{V}_A, \mathbf{V}_R$

 $s^2 c^2 =$ 

Radiative corrections to electroweak observables were expressed in LEPTOP through three functions  $V_i$ :

$$\frac{m_W}{m_Z} = c + \frac{3\bar{\alpha}c}{32\pi s^2(c^2 - s^2)} V_m ,$$

$$g_A = -\frac{1}{2} - \frac{3\bar{\alpha}}{64\pi c^2 s^2} V_A ,$$

$$\frac{g_V}{g_A} = 1 - 4s^2 + \frac{3\bar{\alpha}}{4\pi (c^2 - s^2)} V_R ,$$

$$\sin^2 \theta_W \cos^2 \theta_W = \frac{\pi \bar{\alpha}}{\sqrt{2}G_\mu m_Z^2} , \quad \bar{\alpha} \equiv \alpha(m_Z) = (128.87)^{-1} ,$$

$$V_i \equiv V_i^{\text{SM}} + \delta_{NP} V_i .$$

Compare with S, T and U variables.

$$T = \frac{3}{16\pi s^2 c^2} \delta_{NP} V_A + \Delta \equiv T' + \Delta \quad ,$$

$$S = \frac{3}{4\pi} [\delta_{NP} V_A - \delta_{NP} V_R] + 4s^2 c^2 \Delta \equiv S' + 4s^2 c^2 \Delta \quad ,$$

$$S + U = \frac{3}{4\pi(c^2 - s^2)} (\delta_{NP} V_m - \delta_{NP} V_R) \equiv S' + U' ,$$

$$\Delta \equiv \frac{1}{\bar{\alpha}} \left[ \Pi_Z'(m_Z^2) - \frac{\Pi_Z(m_Z^2)}{m_Z^2} + \frac{\Pi_Z(0)}{m_Z^2} \right] ,$$

### $\mathbf{S}, \mathbf{T}, \mathbf{U} \text{ versus } \mathbf{V}_m, \mathbf{V}_A, \mathbf{V}_R$

#### **Numbers**

#### Table 2

	$m_H = 120$		$m_H = 600$	
	$m_U = 230$	$m_N = 120$	$m_U = m_D = 225$	$m_N = 50$
	$m_D = 220$	$m_E = 200$		$m_E = 200$
T'	-0.001	0.11	-0.006	0.25
T	0.005	0.12	0	0.38
<i>S</i> ′	0.15	-0.01	0.15	-0.23
S	0.15	-0.01	0.16	-0.14

# **Tevatron Higgs search**

"Combined Tevatron upper limit on gg - > H and constraints on the Higgs boson mass in 4th generation fermion models." arXiv:1005.3216v2 (20 May)

- Cross-section of Higgs production in gluon fusion process is increased by a factor of 9
- SM-like Higgs with a mass between 131 Gev and 204 Gev is excluded

# Conclusions

- One extra generation with adjusted masses does not contradict to precision data
- New generation remove upper bound on Higgs
- Strong bounds on Higgs mass with 4th generatin from Tevatron
- Very soon!! LHC will fix  $N_g = 3$  or  $N_g = 4$

# **Global problems with loops**

 Landau pole for Higgs self-coupling, for Yukawa and U(1) coupling

 $\begin{array}{c} & \downarrow \\ \text{Cut-off } \Lambda \\ \text{for New Physics scale} \end{array}$ 

2. Non-Stable Universe

Heavy Fermions contribution to  $V_{higgs}^{eff}$  is negative and makes Universe unstable.

$$V_{higgs}^{eff}(\Phi) \sim \lambda_{eff}(\Phi) \Phi^4$$

 $\lambda(\Phi)$  is negative at large  $\Phi$ .

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