

# *Evidence of CP-violation in MSSM: scenarios with nondegenerate mass parameters of the squark sector*

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# Online

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- **Introduction**
- **Effective THDM potential with explicit CP violation**
- **Parameters of the effective potential**
- **Higgs bosons masses, intense-coupling regime**
- **Decay widths**
- **Summary**

## THDM: Fields

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$$\Phi_1 = \begin{pmatrix} \phi_1^+(x) \\ \phi_1^0(x) \end{pmatrix} = \begin{pmatrix} -i\omega_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \eta_1 + i\chi_1) \end{pmatrix},$$

$$\Phi_2 = e^{i\xi} \begin{pmatrix} \phi_2^+(x) \\ \phi_2^0(x) \end{pmatrix} = e^{i\xi} \begin{pmatrix} -i\omega_2^+ \\ \frac{1}{\sqrt{2}}(v_2 e^{i\zeta} + \eta_2 + i\chi_2) \end{pmatrix}$$

$$\langle \Phi_1 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_1 \end{pmatrix}, \quad \langle \Phi_2 \rangle = \frac{e^{i\xi}}{\sqrt{2}} \begin{pmatrix} 0 \\ v_2 e^{i\zeta} \end{pmatrix} \equiv \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_2 e^{i\theta} \end{pmatrix}.$$

$$\operatorname{tg} \beta = \frac{v_2}{v_1}, \quad v^2 \equiv v_1^2 + v_2^2 = (246 \text{ GeV})^2.$$

# Effective THDM potential with explicit CP violation

The most general renormalized  $SU(2) \times U(1)$  invariant potential

$$U(\Phi_1, \Phi_2) = -\mu_1^2(\Phi_1^\dagger \Phi_1) - \mu_2^2(\Phi_2^\dagger \Phi_2) - \mu_{12}^2(\Phi_1^\dagger \Phi_2) - \mu_{12}^{*2}(\Phi_2^\dagger \Phi_1) +$$

$$+ \frac{\lambda_1}{2}(\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2}(\Phi_2^\dagger \Phi_2)^2 + \lambda_3(\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4(\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) +$$

$$\begin{aligned} \Phi_1^\dagger \Phi_2 &\xrightarrow{CP} \Phi_2^\dagger \Phi_1 \\ \lambda_{5,6,7} &\xrightarrow{CP} \lambda_{5,6,7} \end{aligned}$$

$$\begin{aligned} &+ \frac{\lambda_5}{2}(\Phi_1^\dagger \Phi_2)(\Phi_1^\dagger \Phi_2) + \frac{\lambda_5^*}{2}(\Phi_2^\dagger \Phi_1)(\Phi_2^\dagger \Phi_1) + \\ &+ \lambda_6(\Phi_1^\dagger \Phi_1)(\Phi_1^\dagger \Phi_2) + \lambda_6^*(\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_1) + \\ &+ \lambda_7(\Phi_2^\dagger \Phi_2)(\Phi_1^\dagger \Phi_2) + \lambda_7^*(\Phi_2^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) \end{aligned}$$

$\mu_{12}^2$ ,  
 $\lambda_5, \lambda_6, \lambda_7$   
 complex

$U$  is CP-invariant at the  $M_{SUSY}$  scale,

because  $\lambda_{5,6,7}=0$



# Scalar sector for MSSM

The main contribution to self-couplings due to Yukawa 3<sup>rd</sup> generation couplings.

The corresponding potential with CPV sources

$$\mathcal{V}^0 = \mathcal{V}_M + \mathcal{V}_\Gamma + \mathcal{V}_\Lambda + \mathcal{V}_{\tilde{Q}},$$

$$\mathcal{V}_M = (-1)^{i+j} m_{ij}^2 \Phi_i^\dagger \Phi_j + M_{\tilde{Q}}^2 (\tilde{Q}^\dagger \tilde{Q}) + M_{\tilde{U}}^2 \tilde{U}^* \tilde{U} + M_{\tilde{D}}^2 \tilde{D}^* \tilde{D},$$

$$\mathcal{V}_\Gamma = \Gamma_i^D (\Phi_i^\dagger \tilde{Q}) \tilde{D} + \Gamma_i^U (i \Phi_i^T \sigma_2 \tilde{Q}) \tilde{U} + \Gamma_i^{*D} (\tilde{Q}^\dagger \Phi_i) \tilde{D}^* - \Gamma_i^{*U} (i \tilde{Q}^\dagger \sigma_2 \Phi_i^*) \tilde{U}^*$$

$$\mathcal{V}_\Lambda = \Lambda_{ik}^{jl} (\Phi_i^\dagger \Phi_j) (\Phi_k^\dagger \Phi_l) + (\Phi_i^\dagger \Phi_j) [\Lambda_{ij}^Q (\tilde{Q}^\dagger \tilde{Q}) + \Lambda_{ij}^U \tilde{U}^* \tilde{U} + \Lambda_{ij}^D \tilde{D}^* \tilde{D}] +$$

$$+ \bar{\Lambda}_{ij}^Q (\Phi_i^\dagger \tilde{Q}) (\tilde{Q}^\dagger \Phi_j) + \frac{1}{2} [\Lambda \epsilon_{ij} (i \Phi_i^T \sigma_2 \Phi_j) \tilde{D}^* \tilde{U} + \text{e.c.}] , \quad i, j, k, l = 1, 2$$

$$\Gamma_{\{1; 2\}}^U = h_U \{-\mu^*; A_U\}, \quad \Gamma_{\{1; 2\}}^D = h_D \{A_D; -\mu^*\}$$

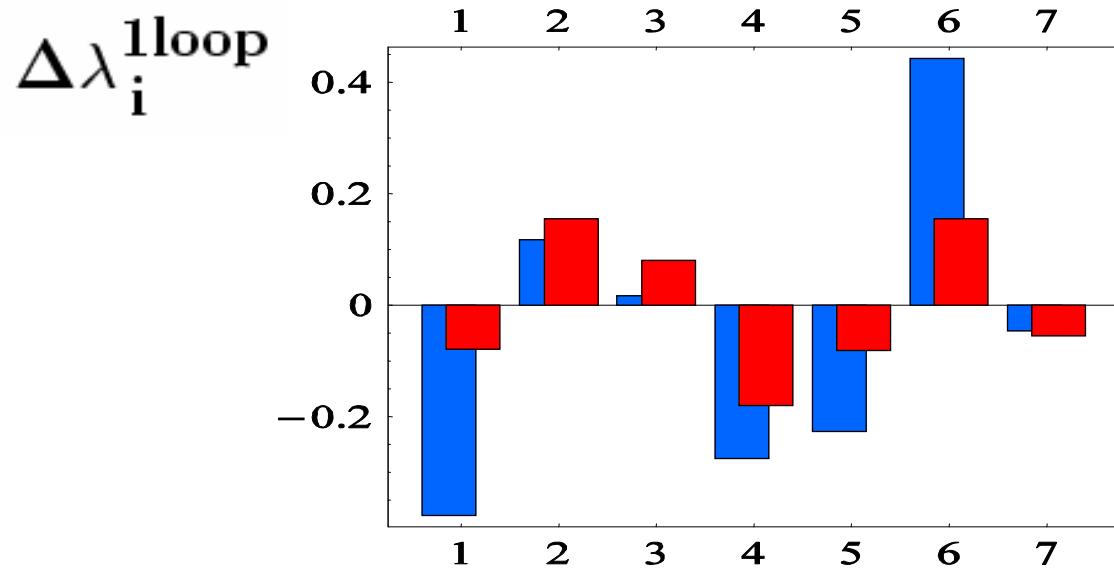
## Parameters of the effective potential

$$\Delta\lambda_5 = 3h_t^4\mu^2 A^2 I_2[m_Q, m_t] + 3h_b^4\mu^2 A^2 I_2[m_Q, m_b]$$

$$\begin{aligned}\Delta\lambda_6 = & -3h_t^4\mu A|\mu|^2 I_2[m_Q, m_t] - 3h_b^4\mu A|A|^2 I_2[m_Q, m_b] + \\ & + h_t^2\mu A\left(\frac{g_1^2 - 3g_2^2}{4}I_1[m_Q, m_t] - g_1^2 I_1[m_t, m_Q]\right) + \\ & + h_b^2\mu A\left(\frac{-12h_b^2 + g_1^2 + 3g_2^2}{4}I_1[m_Q, m_b] - \frac{6h_b^2 - g_1^2}{2}I_1[m_b, m_Q]\right)\end{aligned}$$

$$\begin{aligned}\Delta\lambda_7 = & -3h_t^4\mu A|A|^2 I_2[m_Q, m_t] - 3h_b^4\mu A|\mu|^2 I_2[m_Q, m_b] + \\ & + h_b^2\mu A\left(-\frac{g_1^2 + 3g_2^2}{4}I_1[m_Q, m_b] - \frac{g_1^2}{2}I_1[m_b, m_Q]\right) + \\ & + h_t^2\mu A\left(\frac{12h_t^2 + g_1^2 - 3g_2^2}{4}I_1[m_Q, m_t] - (3h_t^2 - g_1^2)I_1[m_t, m_Q]\right)\end{aligned}$$

# Parameters of the effective potential



■  $M_{\text{susy}} = 500 \text{ GeV}$

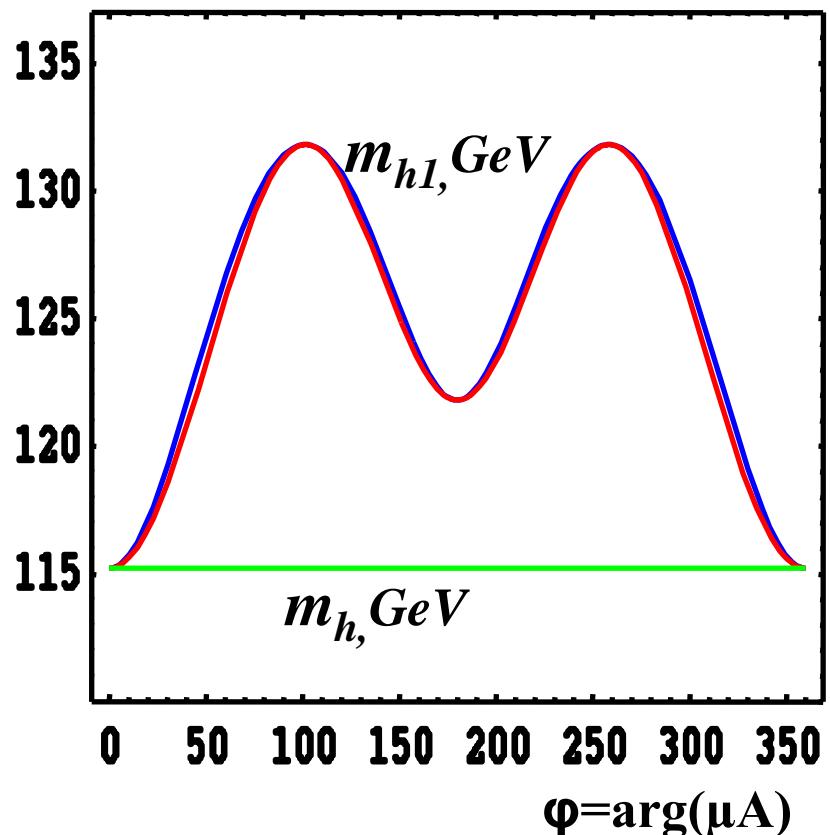
■  $m_Q = 500 \text{ GeV}, m_U = 800 \text{ GeV}, m_D = 200 \text{ GeV}$

[1] H.E.Haber, R.Hempfling, Phys.Rev. D48 (1993) 4280

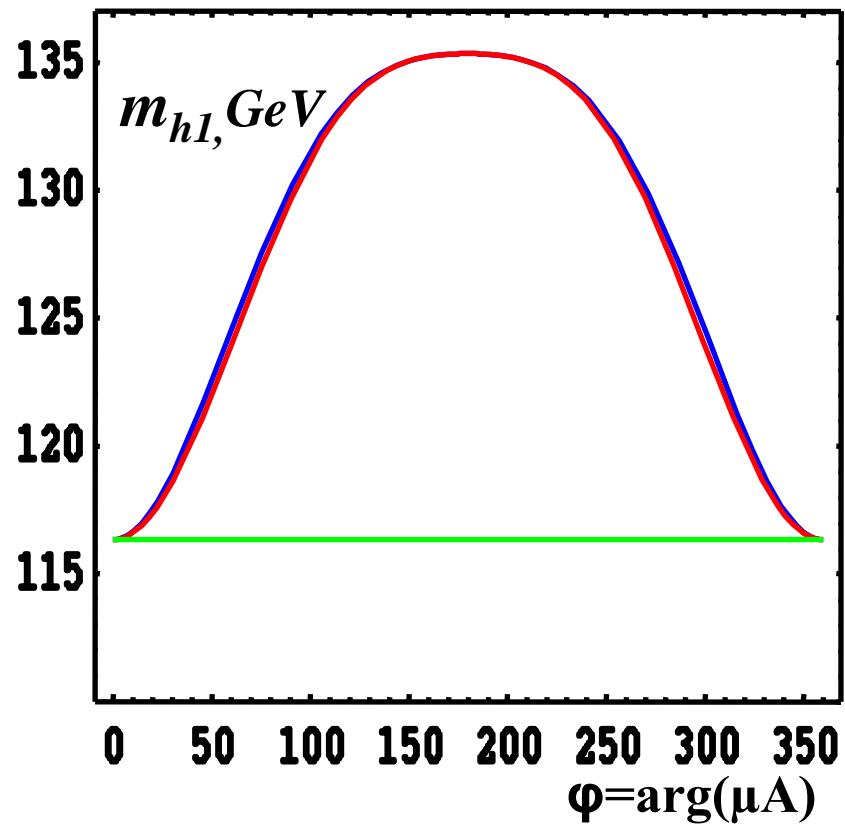
[2] A.Pilaftsis, C.E.M.Wagner, Nucl.Phys. B553 (1999) 3

[3] E.A., M.Dolgopolov, M.Dubinin, Phys.Rev. D71 (2005) 075008

# Mass of the lightest Higgs boson

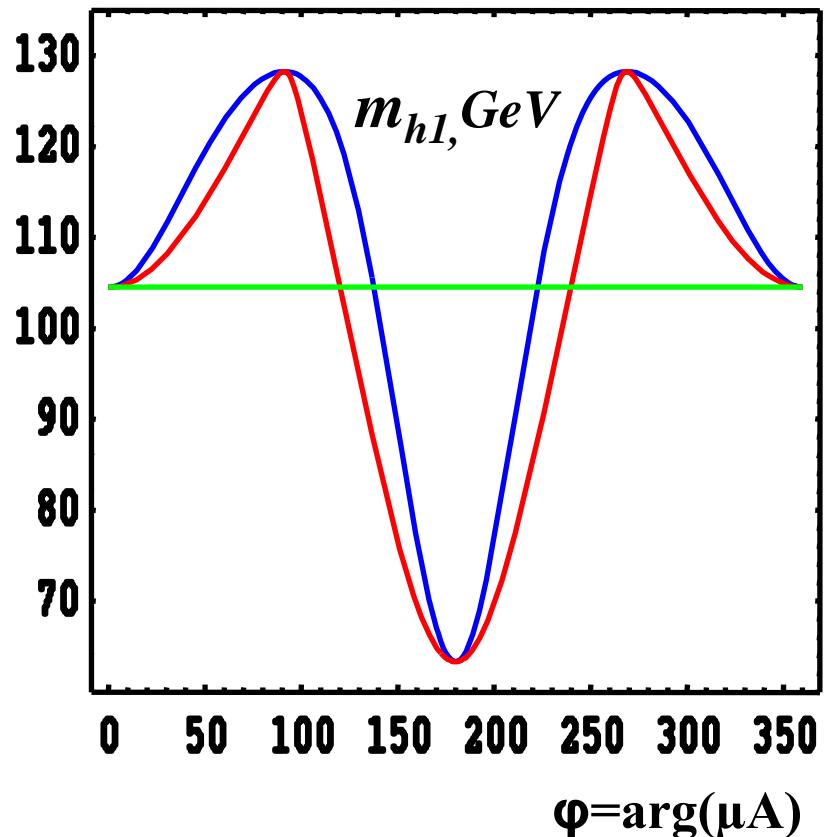


$M_{\text{susy}} = 500 \text{ GeV}$   
 $m_{H^\pm} = 300 \text{ GeV}$

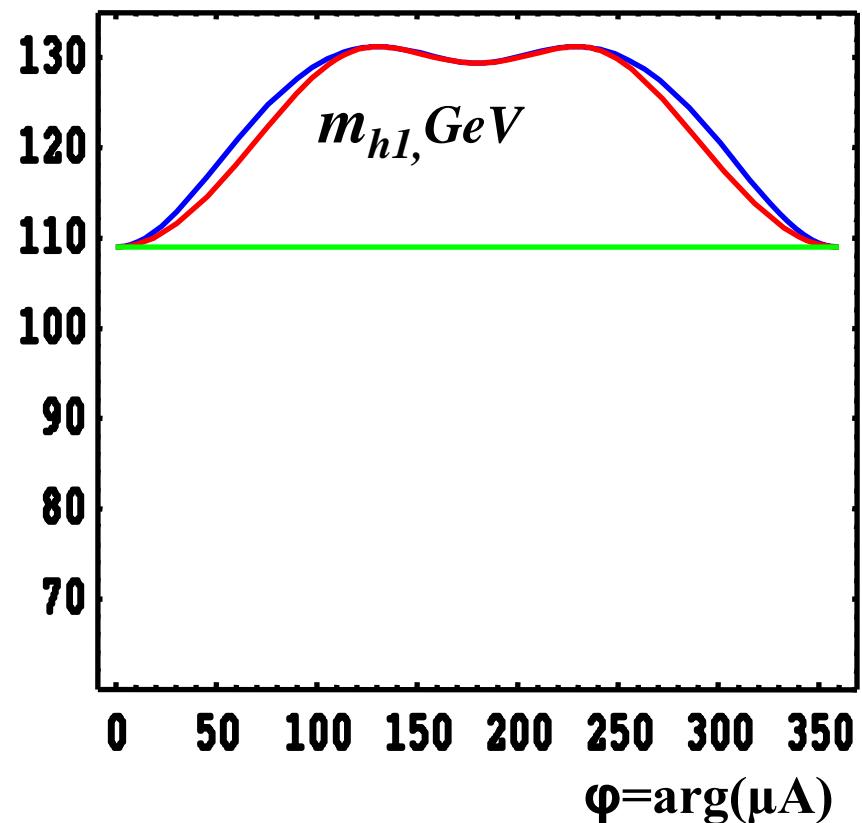


$m_Q = 500 \text{ GeV}, m_U = 800 \text{ GeV},$   
 $m_D = 200 \text{ GeV}$

# Mass of the lightest Higgs boson

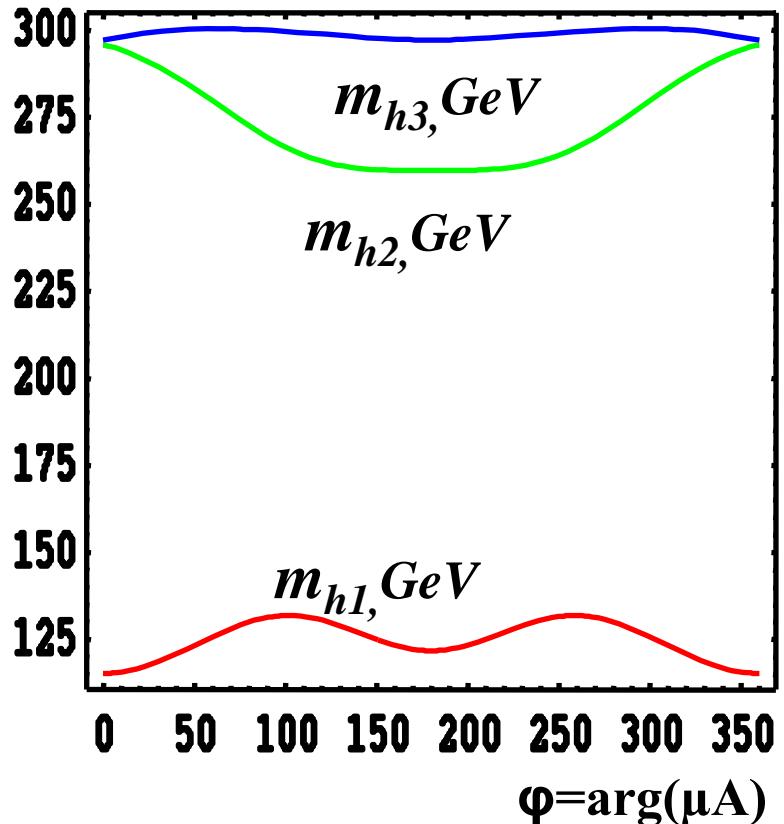


$M_{susy}=500\text{GeV}$   
 $m_{H^\pm}=190\text{GeV}$

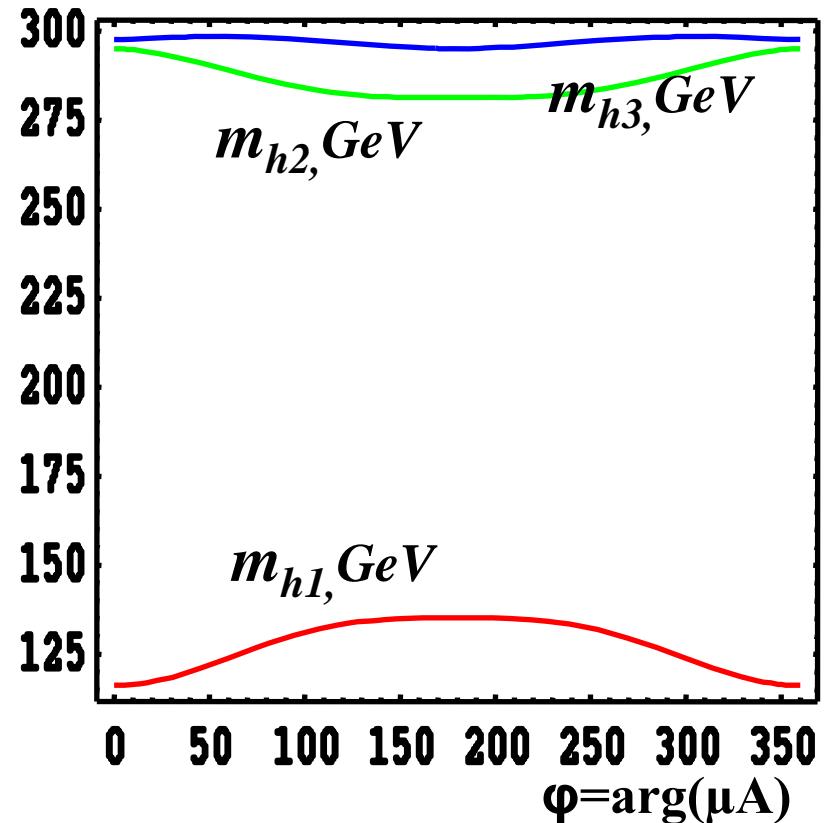


$m_Q=500\text{GeV}, m_U=800\text{GeV},$   
 $m_D=200\text{GeV}$

# Masses of the Higgs bosons

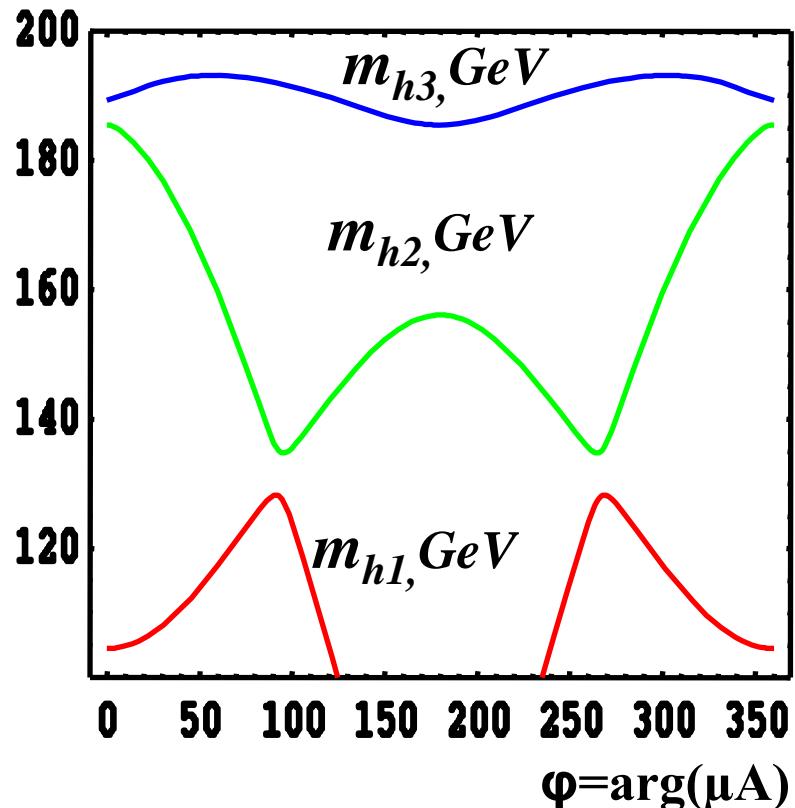


$M_{susy} = 500\text{GeV}$   
 $m_{H^\pm} = 300\text{GeV}$

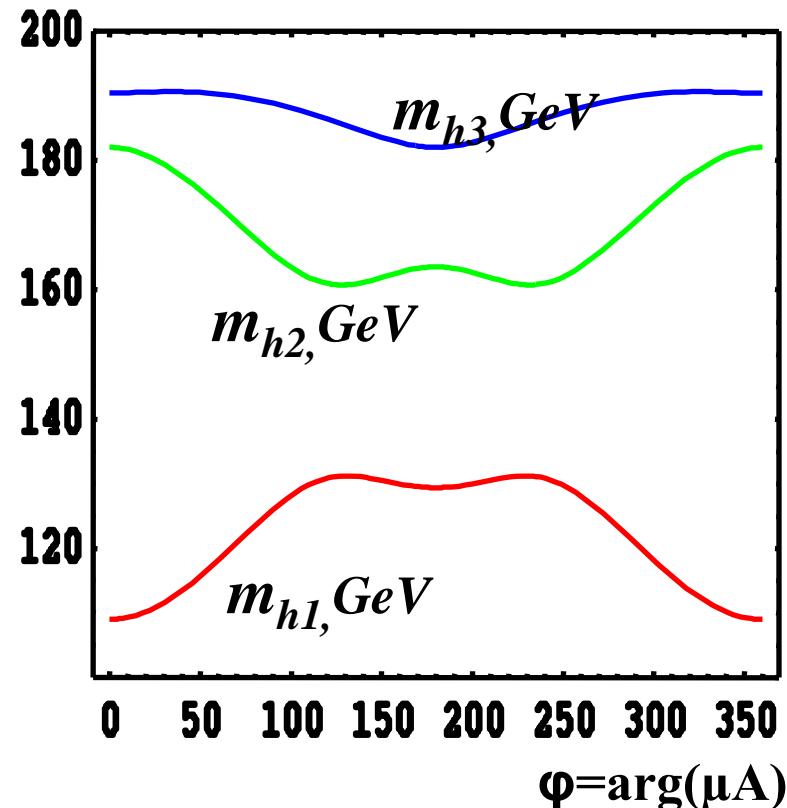


$m_Q = 500\text{GeV}$ ,  $m_U = 800\text{GeV}$ ,  
 $m_D = 200\text{GeV}$

# Masses of the Higgs bosons

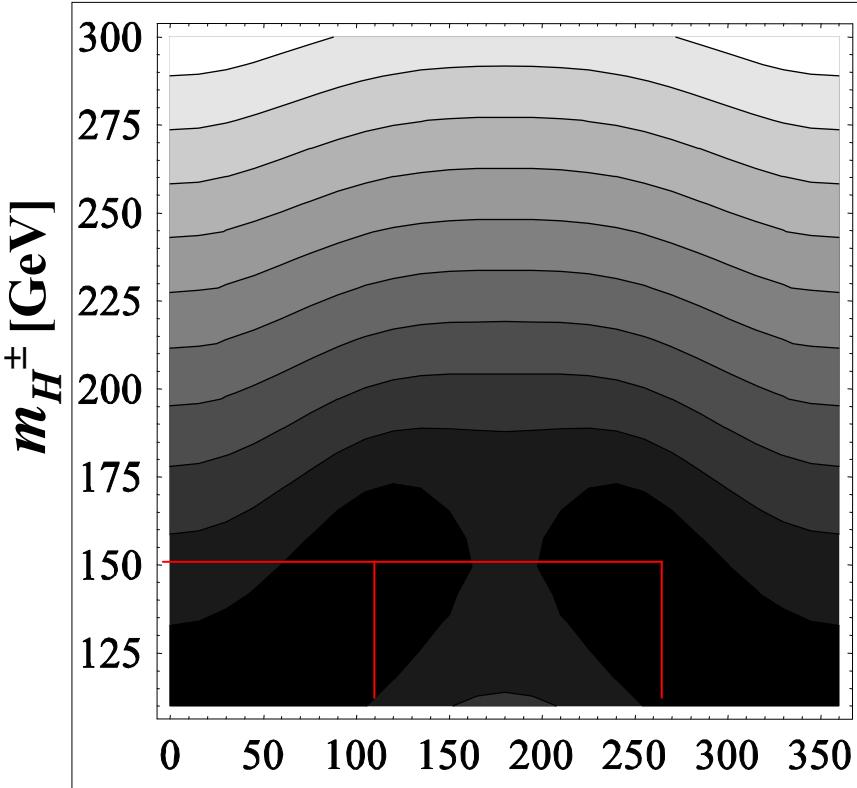


$M_{susy}=500\text{GeV}$   
 $m_{H^\pm}=190\text{GeV}$



$m_Q=500\text{GeV}$ ,  $m_U=800\text{GeV}$ ,  
 $m_D=200\text{GeV}$

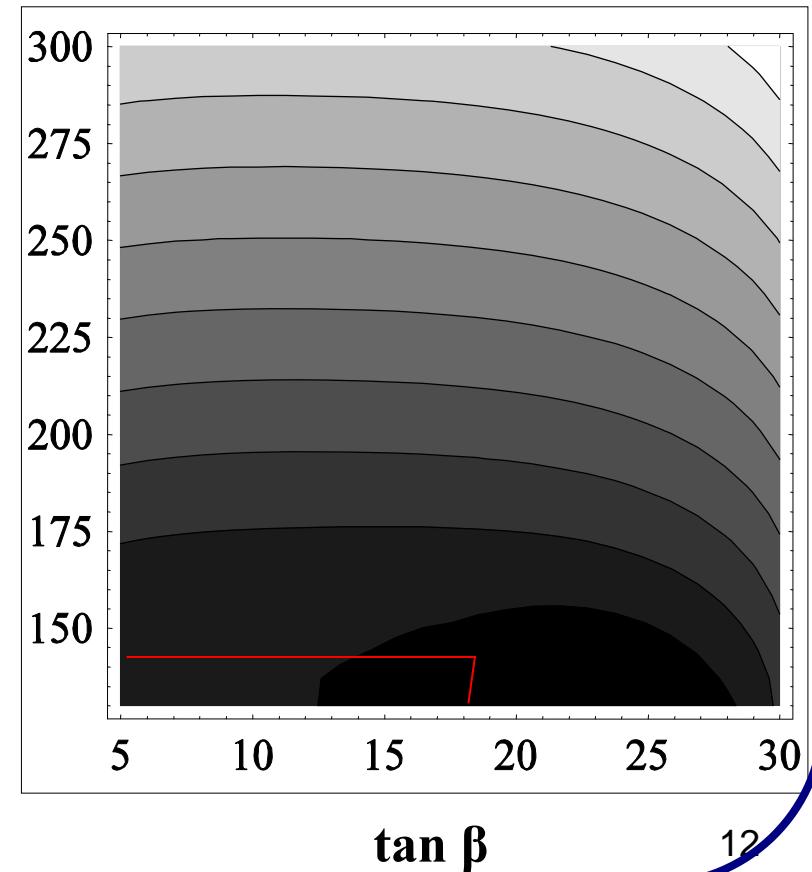
# Masses of the Higgs bosons



$\varphi = \arg(\mu A)$  [rad]

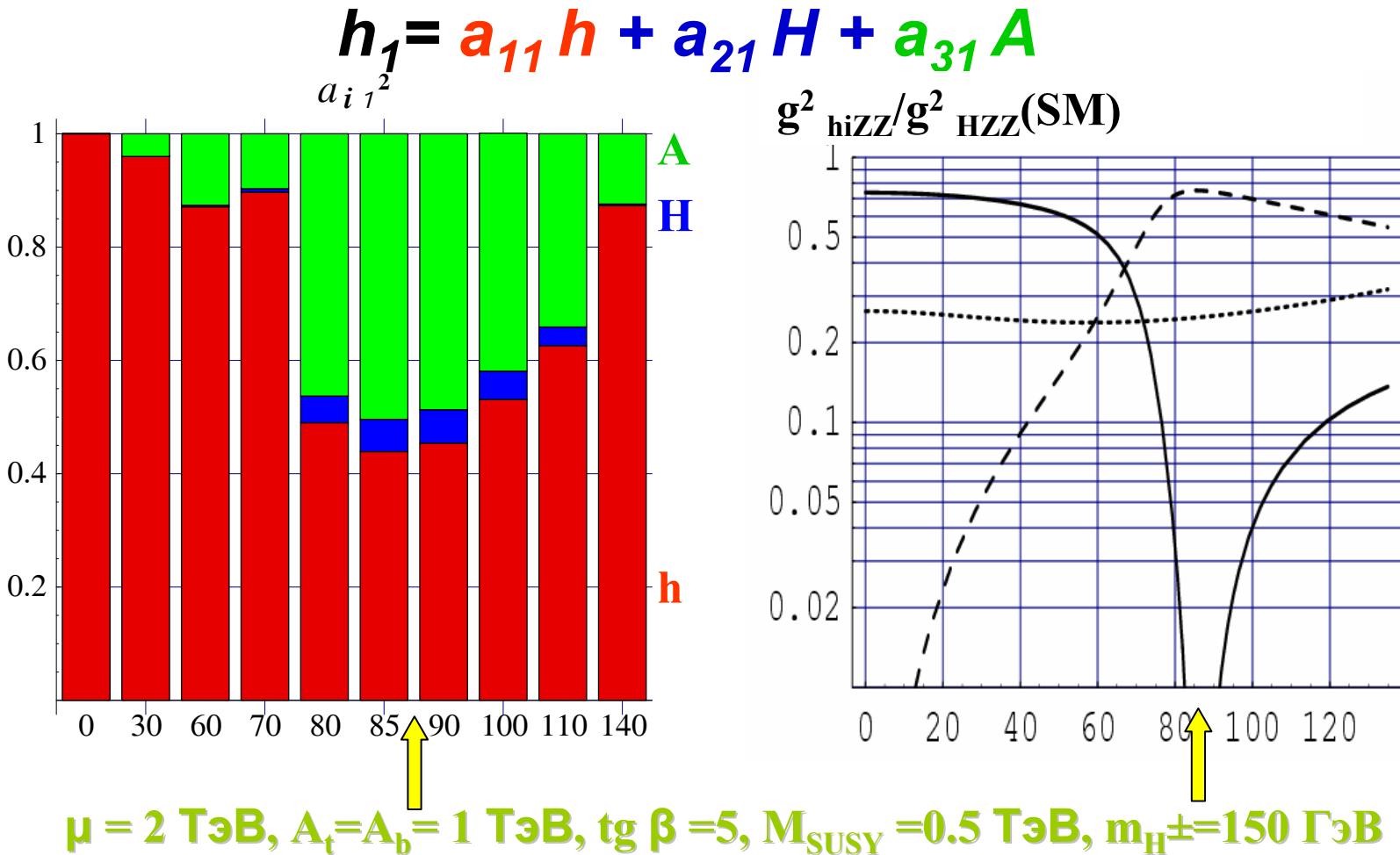
CPX,  $\tan \beta = 5$

$(m_{h2} + m_{h3})/2 - m_{h1}$   
CPX,  $\varphi = 1.4$  [rad]

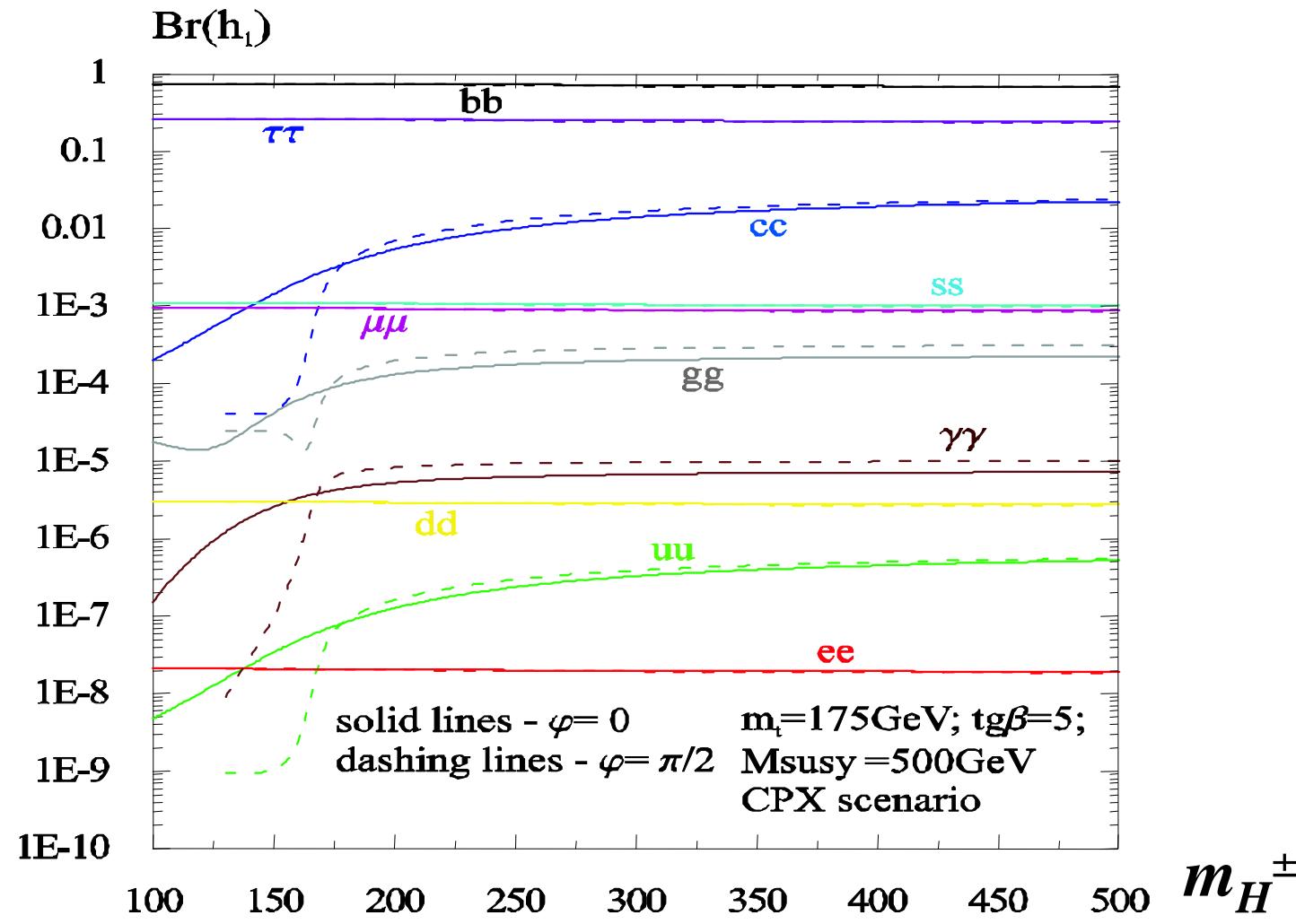


$\tan \beta$

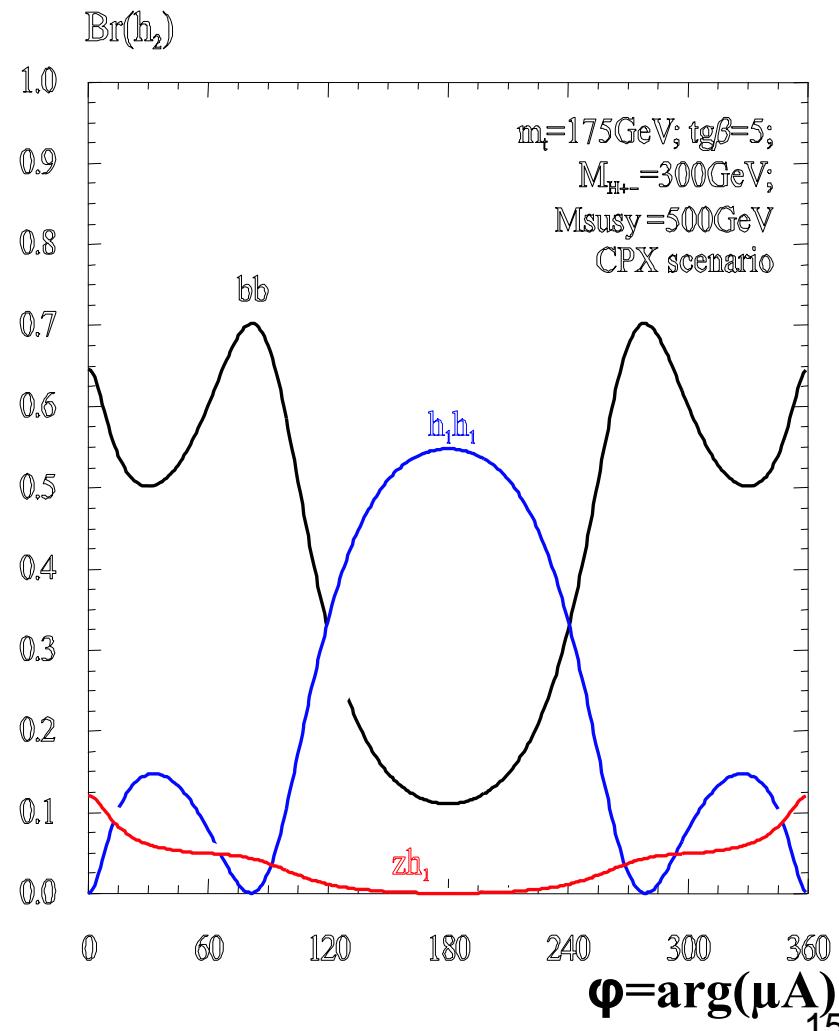
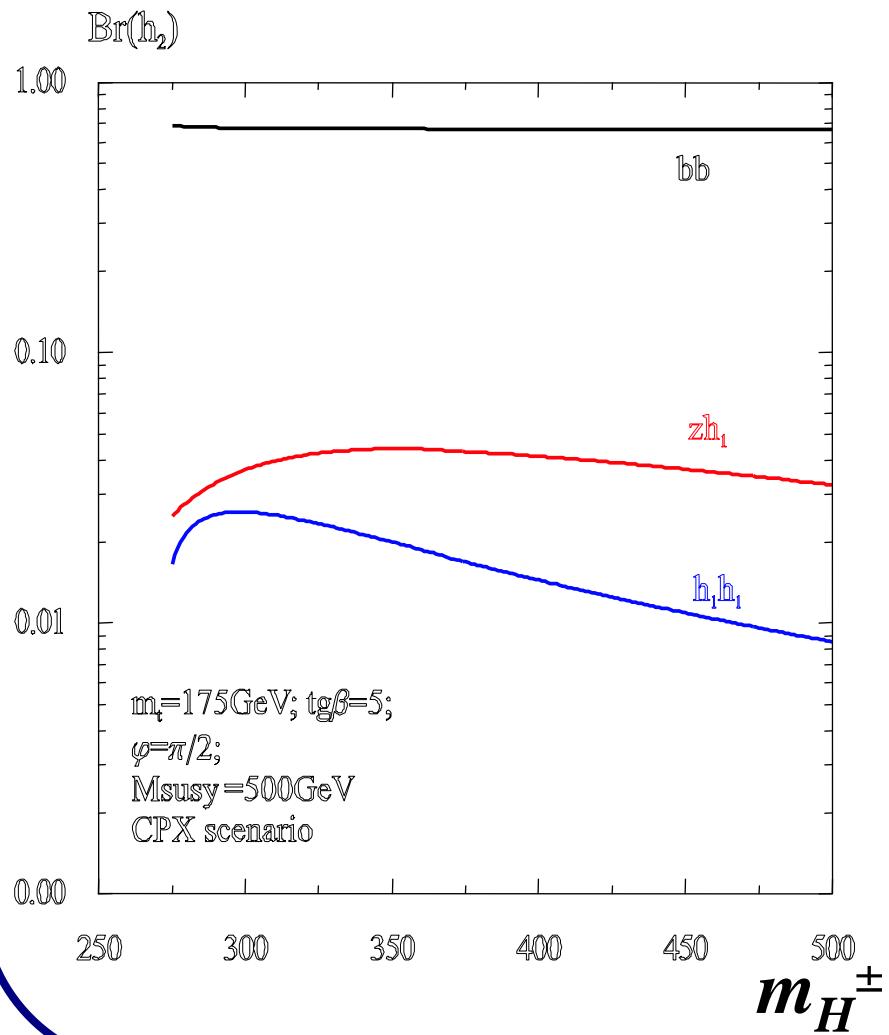
# Matrix elements $a_{i1}$ and coupling with Z-boson



# Branching ratios



# Branching ratios



# ELECTROWEAK BARYOGENESIS

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**Baryon asymmetry in the present Universe**

$$\eta_B \equiv \frac{n_B}{s} = (8.7 \pm 0.3) \cdot 10^{-11}$$

$$\frac{n_B}{n_\gamma} = 6.1 \cdot 10^{-10}$$

**from cosmic microwave background and  
large scale structure**

**in reasonable agreement with  
primordial nucleosynthesis**

# Sakharov's Conditions for Baryogenesis

- *Necessary requirements for baryogenesis:*
  - Baryon number violation
  - CP violation
  - Non-equilibrium
  - $\Rightarrow \Gamma(\Delta B > 0) > \Gamma(\Delta B < 0)$
- **Possible new consequences in**
  - Proton decay
  - CP violation

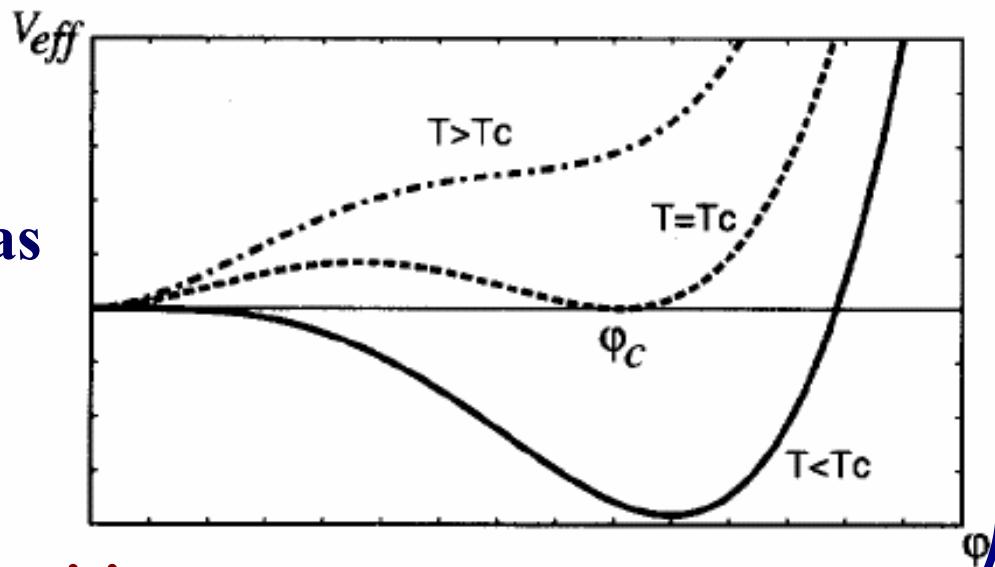
# Condition of the strong first order transition

The first order phase transition is needed for a bubble nucleation.

The sphaleron transition rate should be suppressed in the broken phase at the critical temperature, in order not to erase the created baryon number.

This condition is expressed as

$$\phi_c/T_c \geq 1$$



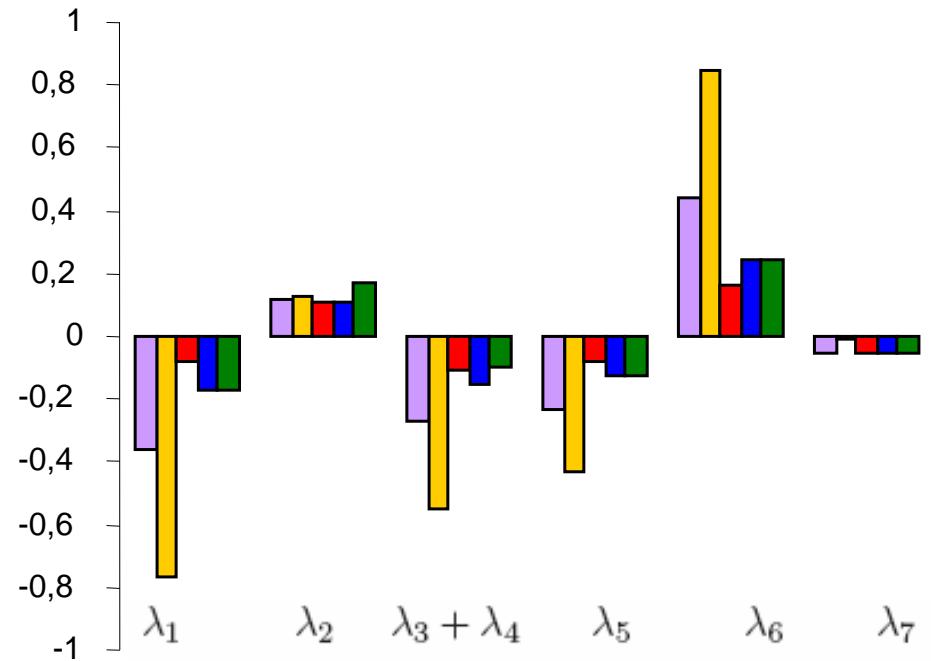
Strong first order phase transition.

# Electroweak Baryogenesis

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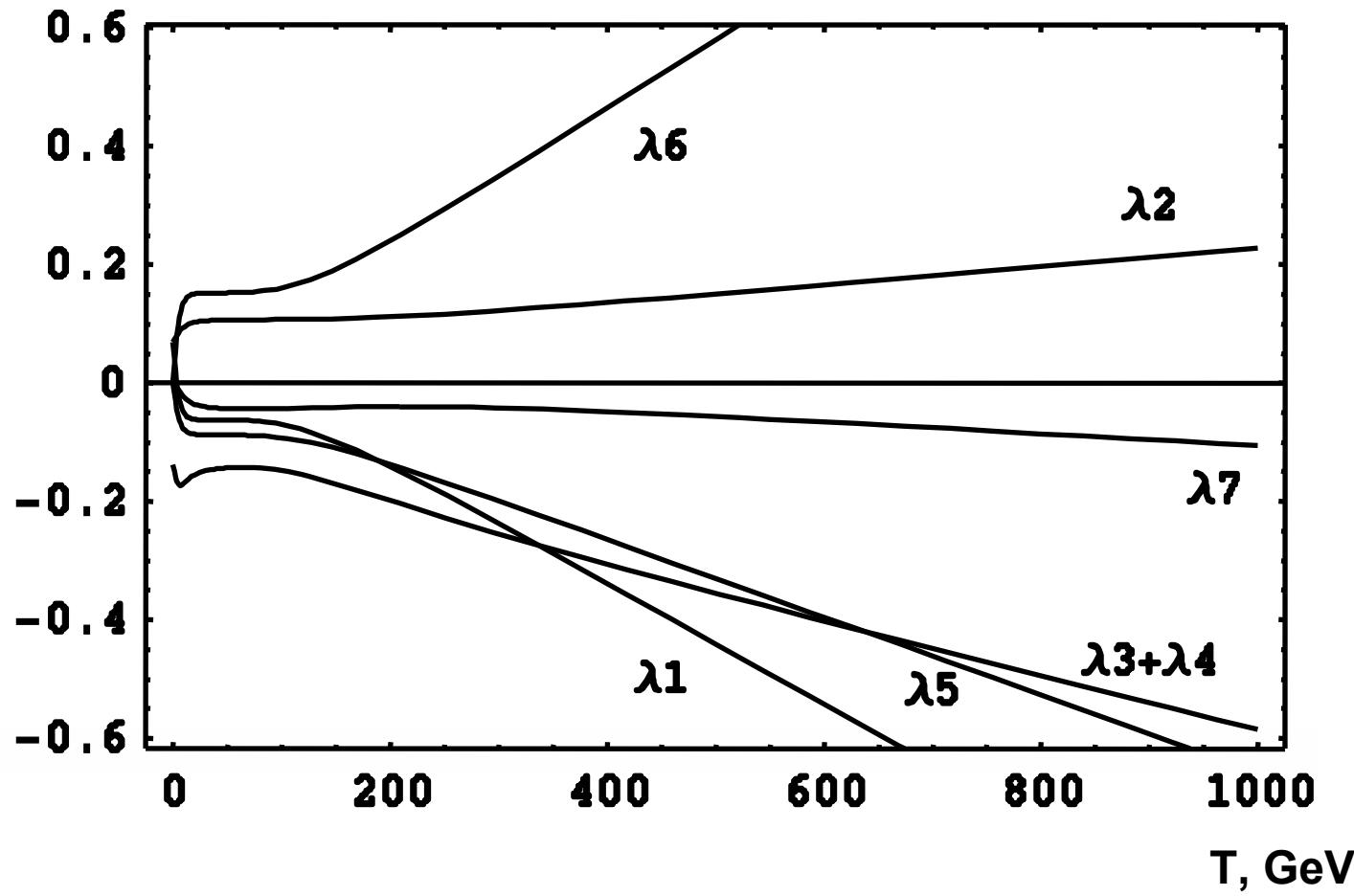
- **Two problems in the Standard Model**
  - First order phase transition requires  $m_h < 50 \text{ GeV}$
  - Need new source of CP violation because
- **Minimal Supersymmetric Standard Model**
  - First order phase transition possible if  $m_{\tilde{t}_R} < 160 \text{ GeV}$
  - New CP violating phase

# Parameters of the finite temperature effective potential

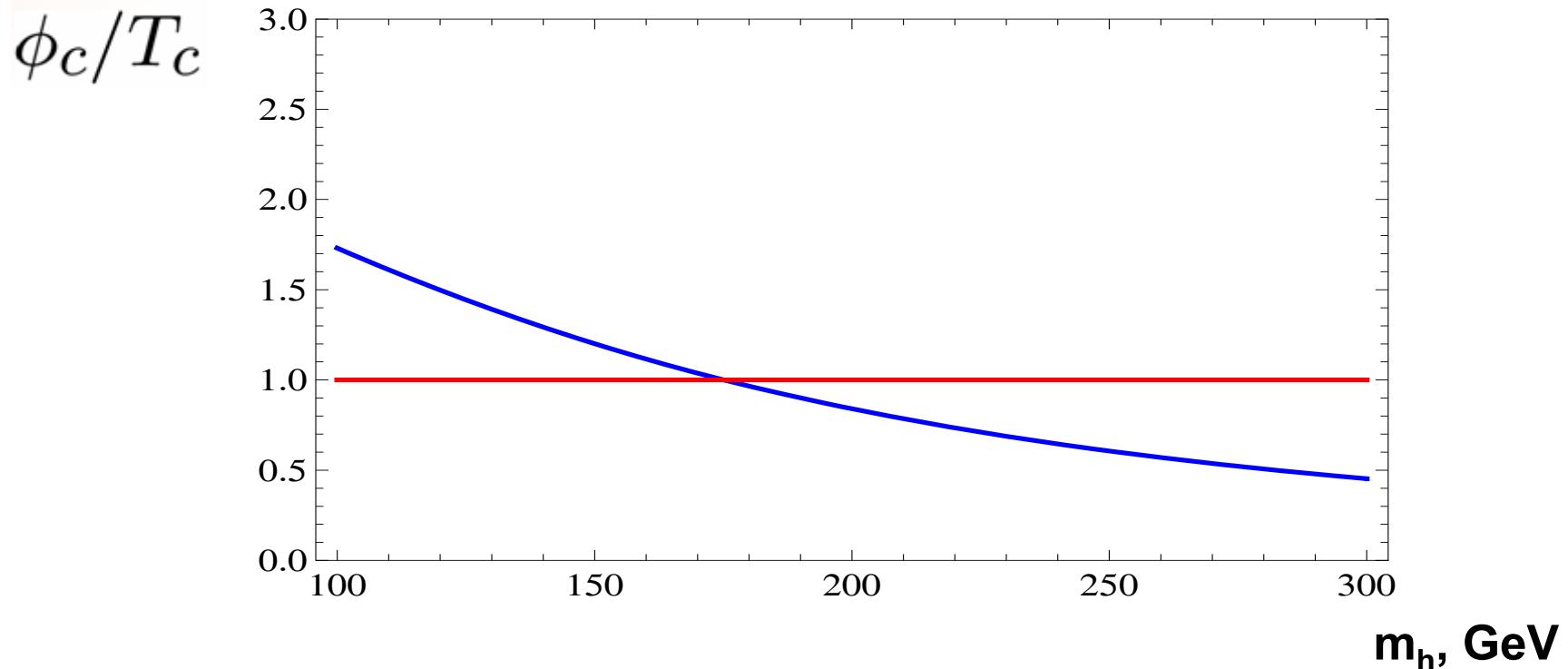


- Msusy=500GeV, T=0.
- Msusy=500GeV, T=200GeV.
- mQ=500GeV, mU=800 GeV, mD=200GeV,T=0.
- mQ=500GeV, mU=800 GeV, mD=200GeV,T=200GeV.
- mQ=500GeV, mU=800 GeV, mD=200GeV,T=200GeV, Log

# Parameters of the effective potential



# $m_h$ in the THDM



$\phi_c/T_c \geq 1$

LEP

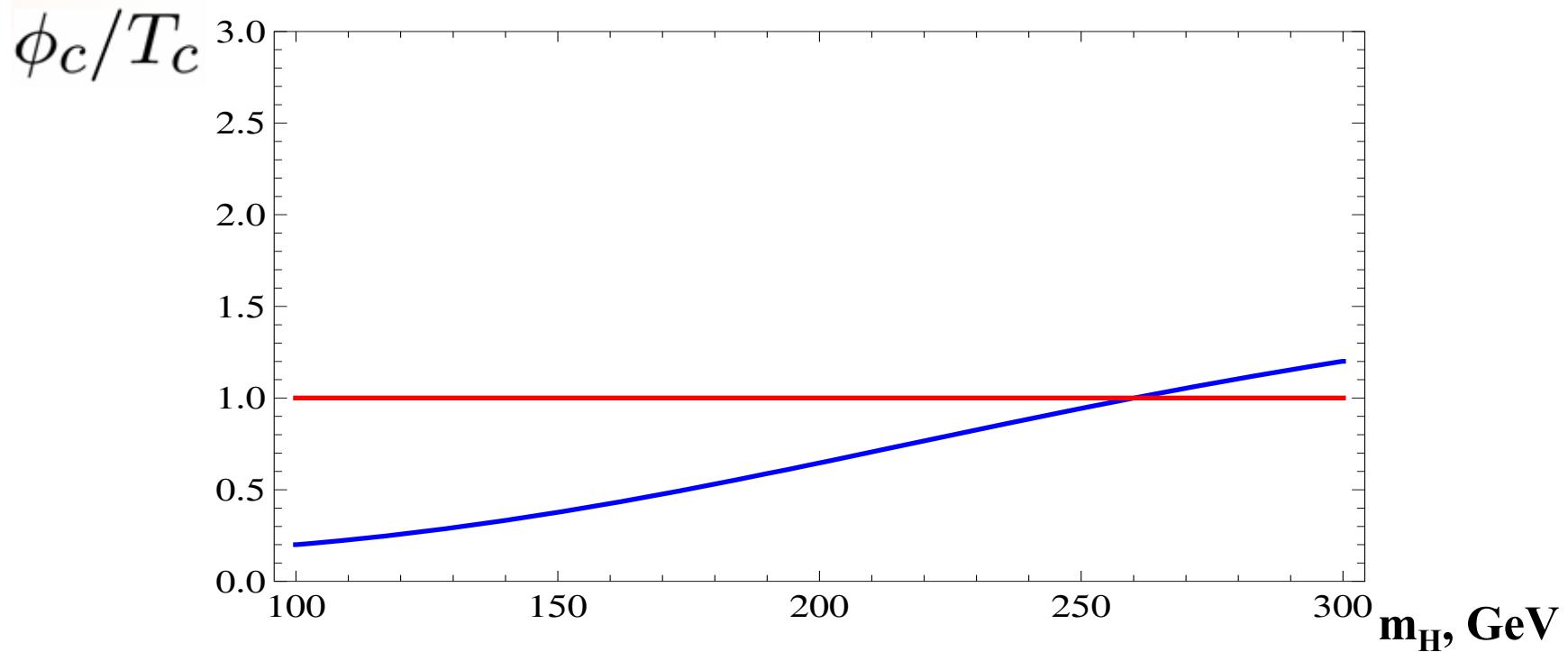


$m_h < 190$  GeV



$m_h > 114.4$  GeV

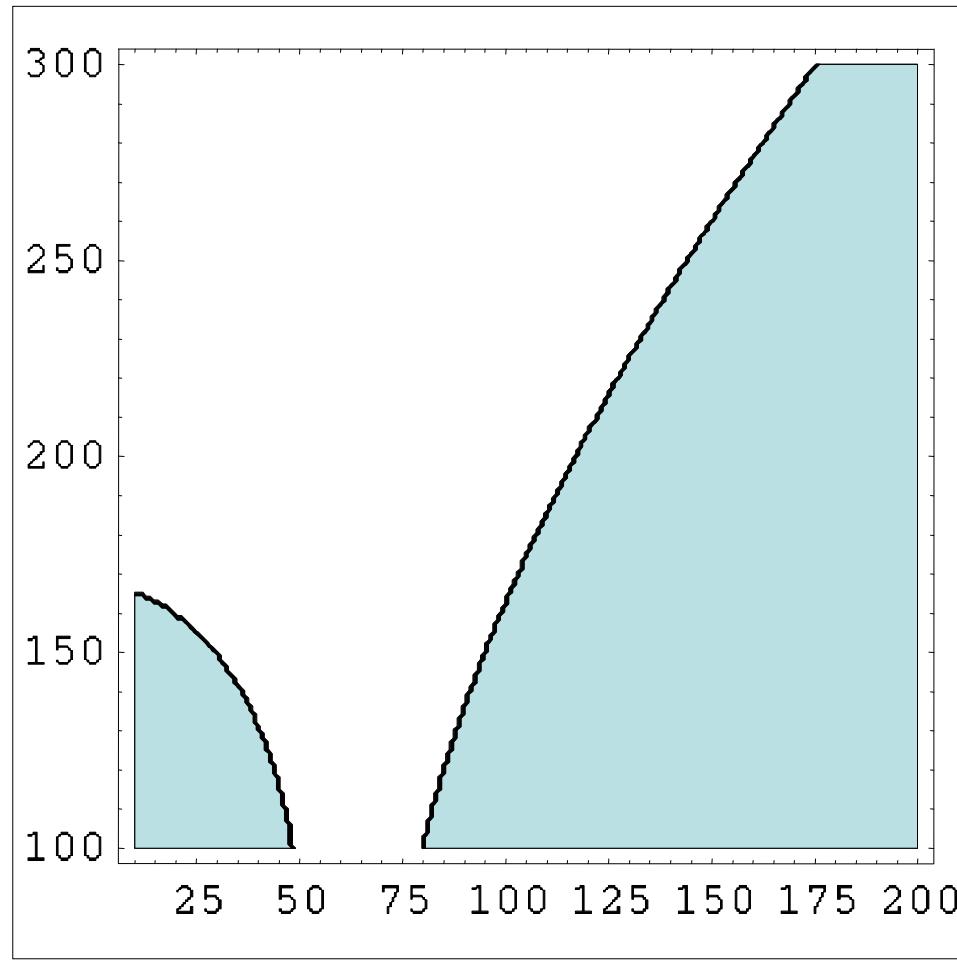
# $m_H$ in the THDM



$\phi_c/T_c \geq 1$     $\rightarrow$     $m_H > 200$  GeV

# $m_h$ and $m_H$ in the THDM

$m_H$ , GeV



$m_h$ , GeV

# Summary

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1. The potential of the THDM in the general case is not CP-invariant and the parameters  $\lambda_{5,6,7}$  of the two-doublet MSSM sector should be taken complex.
2. The deviations of the observable effects in the scenario with nongenerate mass of the squark sector from the phenomenology of the standard scenario can be substantial mainly due to changed masses in comparison with the case of generate scalar quarks mass.
3. The deviations are particularly strong if the power terms  $|\mu A_t|/M_{\text{SUSY}}$  are large and the charged Higgs boson mass does not exceed 150-200 GeV, being rather weakly dependent on the value of  $\tan \beta$ .
4. Such models could lead in principle to a reconsideration of the experimental properties for the signal of the Higgs boson production at the modern and future colliders.