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# Hybrid Models of Supersymmetry Breaking

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# Outline

- Gravity and gauge mediation: advantages/problems
- Hybrid models and metastability
- Hybrid models with GUT induced doublet-triplet messenger splitting
- Prospects

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# 1. Gravity and gauge mediation : advantages/problems

## - Gravity mediation

SUSY broken in a "hidden" sector which communicates with our sector via (super)gravitational interactions

$$\begin{array}{ccc} \text{MSSM} & \leftrightarrow & \text{Hidden Sector} \\ & \text{nonren.int.} & T_i, \langle F_i \rangle \neq 0 \end{array}$$

Define  $F^2 = \sum_i |F_i|^2$ , then

$$M_{SUGRA} \sim m_{3/2} \quad , \quad m_{3/2} = \frac{F}{\sqrt{3}M_P}$$

Ex :  $(G = K + \ln |W|^2, F^\alpha = m_{3/2} G^\alpha)$

$$m_{i\bar{j}}^2 = m_{3/2}^2 (G_{i\bar{j}} - R_{i\bar{j}\alpha\bar{\beta}} G^\alpha G^{\bar{\beta}})$$

## Advantages:

- Natural solution for the  $\mu$ -problem via Giudice-Masiero mechanism

$$\mu \sim m_{3/2} \quad , \quad B\mu \sim m_{3/2}^2$$

where

$$L_{MSSM} = (\int d^2\theta \mu H_1 H_2) + B\mu h_1 h_2 + c.c. + \dots$$

- Easy to construct explicit models, natural in [string theory](#) (moduli fields)

## Problems

- FCNC effects are generically problematic in SUGRA theories (GIM not enough)

Solutions for FCNC problem :

- i) **flavor universality** :  $(m_0^2)_{ij} = (m_0^2)\delta_{ij}$
- ii) **alignement** :  $(m_0^2)_{ij}$  are aligned to Yuk.  $Y_{ij}$   
(diagonalized in the same basis)

If not squark, slepton masses  $> 50$  TeV or so !

- Universality/alignment are **not generic** in gravity mediation.

- **Gauge** mediation

Transmission of SUSY breaking through **SM gauge loops**  
= gauge mediation

$$\begin{array}{ccccc} \text{SUSY breaking} & \leftrightarrow & \text{Messenger} & \leftrightarrow & \text{MSSM} \\ \text{sector} & & \text{sector} & & \\ X = \langle X \rangle + \theta^2 F_X & \rightarrow & X \Phi \tilde{\Phi} & \rightarrow & \text{soft terms} \end{array}$$

Messengers are typically :

- vector-like, charged under SM gauge group.
- If  $SU(5)$  complete multiplets (say  $N$  pairs  $5 + \bar{5}$ ), they preserve MSSM gauge coupling unification.

- MSSM **soft terms**, minimal gauge mediation:
  - gaugino masses  $\rightarrow$  **1-loop**

$$M_{1/2} \sim N_m \frac{g^2}{16\pi^2} \left( \frac{F_X}{\langle X \rangle} \right) \sim N_m M_{GMSB}$$

- scalar (squarks, sleptons) masses : **two-loops**

$$m_0^2 \sim N_m \left( \frac{g^2}{16\pi^2} \right)^2 \left( \frac{F_X}{\langle X \rangle} \right)^2 \sim N_m M_{GMSB}^2$$

Typically  $M_{GMSB} \gg m_{3/2}$ , gravitino very light (**LSP**)

Minimal gauge mediation has

- $Str M^2 = 0$  in the messenger sector.
- $SU(5)$  symmetric messenger masses.

Advantages :

- Gauge mediation solves the **flavor problem**
- In its minimum version, highly predictive spectrum.

Problems :

- Very **difficult** to generate  $\mu$ ,  $B\mu$  of correct size.
- Complicated explicit models (**vacuum metastability**) .

## 2. Hybrid models

(Poppitz-Trivedi,..., Mambrini,Pokorski,Romagnoni,E.D.  
; Feng, Lester and Nir ; Lavignac, Parmentier and E.D.)

In recent works messengers are taken to be **very heavy**

$$\mathcal{M}_m \sim 10^{13} - 10^{16} GeV$$

Then  $m_{3/2} \sim M_{GMSB}$  is possible and the SUGRA and GMSB contributions can be **comparable**.

$$m_0^2 \sim m_{3/2}^2 + N_m M_{GMSB}^2 ,$$

$$M_{1/2} \sim m_{3/2} + N_m M_{GMSB}$$

Couplings of messengers to SUSY breaking sector:

$$W_m = \Phi(\lambda_X X + \mathcal{M})\tilde{\Phi}$$

where  $X$  is the SUSY breaking field(s).

Gauge / SUGRA contributions to MSSM soft terms

$$\frac{M_{GMSB}}{m_{3/2}} \sim N_m \frac{g^2}{16\pi^2} \lambda_X \frac{M_P}{\mathcal{M}}$$

can be comparable for **very heavy messengers**.

Most models are **metastable** (lower vacuum with messenger vev's); lifetime of our vacuum

$$\tau \sim e^{\frac{1}{\lambda_X^2}}$$

- **Stability** prefers gravity mediation.

- Hybrid models could combine **advantages** of both SUSY breaking mechanisms if

$$M_{GMSB} \sim TeV \sim 30 - 100 m_{3/2} \quad (1)$$

We use ISS (Intriligator-Seiberg-Shih) model as sector that breaks SUSY (other DSB models similar results).

$$W = W_{ISS} + W_m + W_\mu + W_{MSSM}$$

$$W_{ISS} = h q X \tilde{q} - h f^2 \text{Tr} X$$

$$W_\mu = \lambda \frac{q \tilde{q}}{M_P} H_1 H_2$$

where  $f^2 = m \Lambda \sim (10^{10} GeV)^2$ .

- $\lambda_X \sim \Lambda/M_P \ll 1 \rightarrow$  large lifetime.

At tree-level there are **pseudo-moduli** in  $X$ . At one-loop, effective potential generates a vev  $\langle X \rangle \sim (\lambda_X^3/h^2)(f^2/\mathcal{M})$ .

$$m_{3/2} \sim \frac{F_X}{M_P}$$
$$\mu \sim \frac{N}{h} m_{3/2} \quad , \quad B = \frac{F_q}{q} \sim h \langle X \rangle$$

We need  $N/h \gg 1$ .  $\mu$  and  $B$  are similar ( $TeV$ ).

### 3. Hybrid models with **GUT induced** doublet-triplet messenger **splitting**

Messengers are naturally very heavy if they couple to  $SU(5)$  GUT adjoint ( $\mathbf{5} \times \bar{\mathbf{5}} = \mathbf{1} + \mathbf{24}$ ). The messenger mass matrix is

$$\mathcal{M} = \lambda_{\Sigma} \Sigma + \lambda'_{\Sigma} \frac{\Sigma^2}{M_P}$$

where  $\Sigma$  is the  $SU(5)$  GUT adjoint breaking  $SU(5) \rightarrow$  SM. If  $\langle X \rangle \ll \langle \Sigma \rangle \sim M_{GUT} \times \text{diag} (2, 2, 2, -3, -3)$ , then doublet and triplet messengers are split

$$\mathcal{M}_{3m} \simeq 2\lambda_{\Sigma} M_{GUT} \quad , \quad \mathcal{M}_{2m} \simeq -3\lambda_{\Sigma} M_{GUT}$$

Messengers are very heavy; it is easy to obtain (1).

Since  $\langle \Sigma \rangle \sim VY$ , we get a peculiar spectrum at high energy :

(Ex:  $M_a^2 \sim (\text{one-loop}) \text{Tr}(Q_a^2 / \langle \Sigma \rangle)$ )

$$M_3 = -\frac{3}{2}M_2 \sim TeV, \quad M_1 \sim 100 GeV$$

$$m_{qL}^2 \simeq \frac{5}{4}m_{uR}^2, \quad m_{dR}^2 \simeq m_{uR}^2$$

$$m_{eL}^2 \simeq \frac{5}{6}m_{eR}^2, \quad m_{uR}^2 \simeq 4m_{eL}^2, \quad \text{etc}$$

$$\mu, B \sim TeV$$

- Bino gets GMSB mass only from  $\lambda'_\Sigma \rightarrow$  bino and the gravitinos are the lightest.
- The other superpartner masses are 300 GeV - 1 TeV.

## Prospects

- LHC will start in 2008 the hunt for physics BSM and particularly low-energy SUSY.
- There are generically three possibilities :
  - generic SUGRA mediation  $\rightarrow$  all soft terms of the same order  $m_{soft} \sim m_{3/2}$ , but numerically different.
  - gauge mediation  $\rightarrow$  flavor universality and some correlation between the different soft terms. Very likely that this will be a metastable vacuum, in which case "There are reasons of anxiety" (Coleman, 1977).

- **hybrid** models : they can combine advantages and eliminate problems of gauge / gravity mediations
  - For **GUT induced** doublet-triplet messenger splitting, predictive spectrum related to existence of  $SU(5)$  GUT.
  - Under investigation : comparison of the low-energy spectrum with minimal gauge mediation and mSUGRA.
  - More general cases deserve attention : **LHC** predictions important !